

# Appendix K

## Example Calculations

Appendix K includes example calculations for the Road Design Manual. The examples are numbered to correspond with the associated chapter material, as described below.

- Sight Distance (Chapter 2)
- Horizontal Alignment (Chapter 3)
- Vertical Alignment (Chapter 4)
- Roadside Safety (Chapter 9)
- Quantity Summaries (Chapter 13)

# Sight Distance Example Calculations

## Example 2-1: Horizontal Sight Distance – Middle Ordinate

**Given:** Design Speed = 60 mph  
 $R = 1,400$  feet

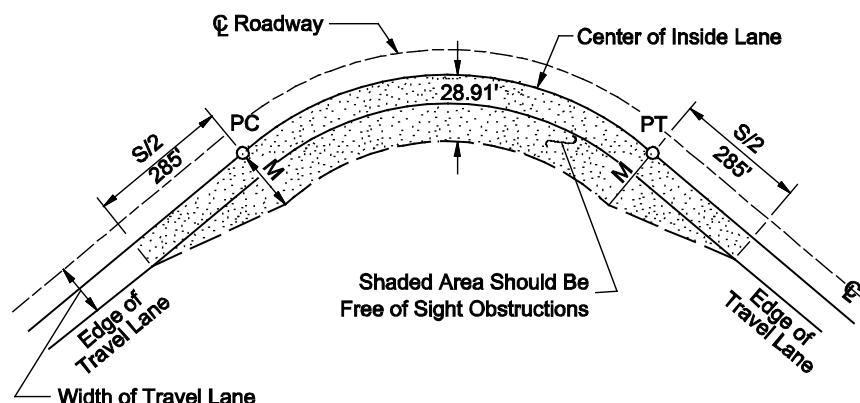
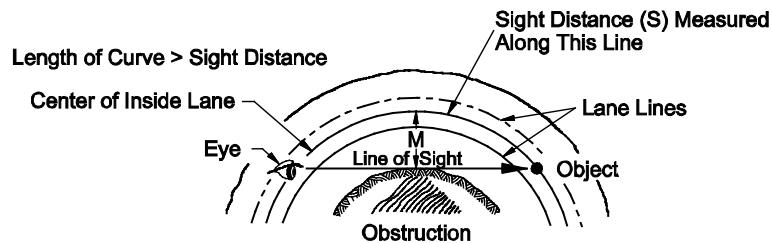
**Problem:** Determine the horizontal clearance requirements for the horizontal curve using the desirable stopping sight distance ( $SSD$ ) value.

**Solution:** Chapter 2, Exhibit 2-1 yields a  $SSD = 570'$ . Using Appendix F, Equation F.2-1 for horizontal clearance:

$$M = R \left( 1 - \cos \left( \frac{90^\circ \cdot S}{\pi \cdot R} \right) \right)$$

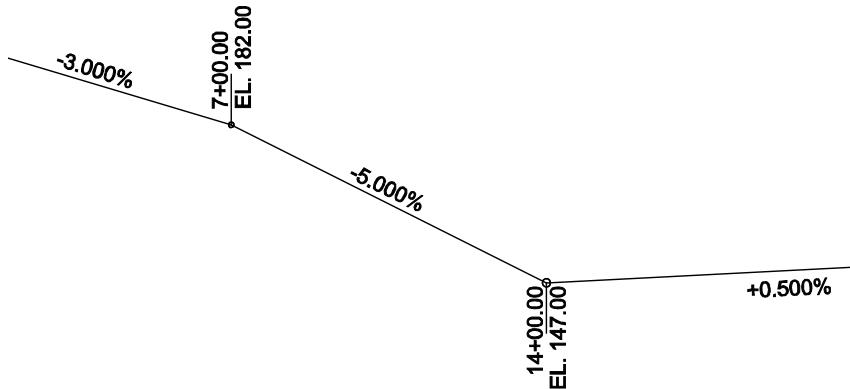
$$M = 1400 \left( 1 - \cos \left( \frac{(90^\circ)(570)}{(\pi)(1400)} \right) \right) = 28.91'$$

The exhibit below illustrates the horizontal clearance requirements for the entering and exiting portion of the horizontal curve.



**Example 2-2: Stopping Sight Distance with Vertical Curves**

**Given:** The grade line for a 60-mph design speed, two-lane, two-way rural roadway is shown below. Give consideration to the effect of grades on *SSD*.



**Problem:** Determine the appropriate profile that meets minimum stopping sight distance, as well as consider passing sight distance for additional refinement.

**Solution:**

1. Since the grades are 3 percent and greater, determine stopping sight distance adjusted for downgrades. The 5-percent grade is the maximum of the downgrades, and will be used for calculating *SSD*. Using Chapter 2, Equation 2.8-3:

$$SSD_{\text{Downgrades}} = 1.47Vt + \frac{V^2}{30 \left[ \left( \frac{a}{32.2} \right) - G \right]}$$

where:

*SSD* = stopping sight distance, feet.

*V* = design speed, mph

*t* = brake reaction time, 2.5 seconds

*a* = deceleration rate, 11.2 foot per second squared

*G* = gradient, feet/feet

$$SSD_{-5\%} = 1.47 \times 60 \times 2.5 + \frac{60^2}{30[(11.2 \div 32.2) - .05]} = 623.4, \text{ Round } \Rightarrow \underline{624'}$$

2. Second, calculate the minimum length for the crest curve for the calculated *SSD* using Equation 4.4-1:

$$L = \frac{AS^2}{200(\sqrt{h_1} + \sqrt{h_2})^2}$$

Where:

*L* = length of vertical curve, feet

*A* = algebraic difference between the two tangent grades, percent

*S* = sight distance, feet

*h*<sub>1</sub> = height of eye above road surface, feet

*h*<sub>2</sub> = height of object above road surface, feet

$$L = \frac{AS^2}{200 \times (\sqrt{h_1} + \sqrt{h_2})^2} = \frac{2 \times 624^2}{2158} = 360.87'$$

3. Since this length is less than the *SSD*, Equation 4.4-2 can be used:

$$L = 2S - \frac{200(\sqrt{h_1} + \sqrt{h_2})^2}{A}$$

Where:

*L* = length of vertical curve, feet

*A* = algebraic difference between the two tangent grades, percent

*S* = sight distance, feet

*h*<sub>1</sub> = height of eye above road surface, feet

*h*<sub>2</sub> = height of object above road surface, feet

$$L = 2S - \frac{200 \times (\sqrt{h_1} + \sqrt{h_2})^2}{A} = 2 \times 624 - (2158 \div 2) = 169'$$

The minimum curve length providing *SSD* is 169 feet, however the minimum curve length based on *L*<sub>min</sub> = 3*V* would be 180 feet.

4. Prior to finalizing the crest curve length, we'll determine the needed length for the sag curve based on *SSD*:

Calculate the minimum length for the sag curve using Equation 4.4-7:

$$L = \frac{AS^2}{200h_3 + 3.5S}$$

Where:

*L* = length of vertical curve, feet

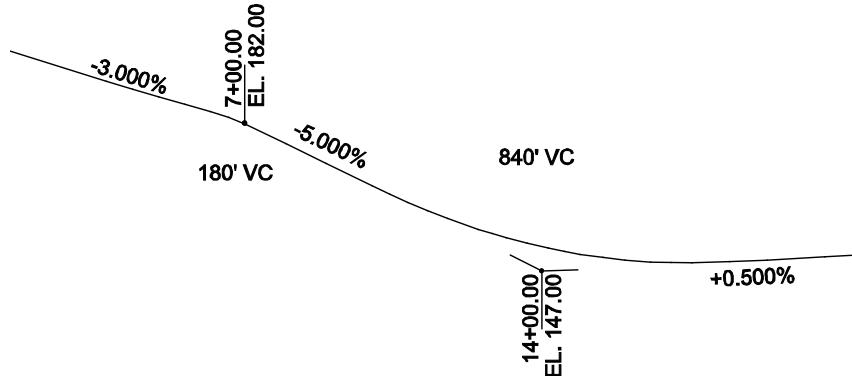
*A* = algebraic difference between the two tangent grades, percent

*S* = sight distance, feet

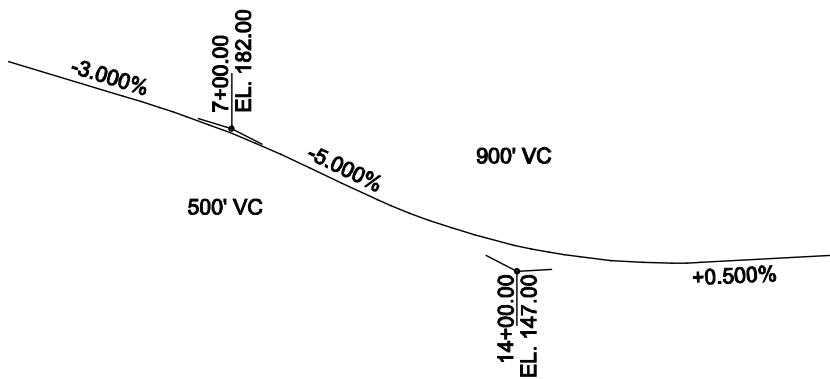
*h*<sub>3</sub> = height of headlights above pavement surface, feet

$$L = \frac{AS^2}{200 \times h_3 + 3.5S} = \frac{5.5 \times 624^2}{200 \times 2 + (3.5 \times 624)} = 828.78'$$

For this example, both curves can be designed to provide *SSD* adjusted for the 5 percent downgrade, using a 180-foot long crest and 840-foot sag curves (lengths rounded up for design), without curve overlap.



**Additional Discussion:** Rather than using the minimum lengths of curve calculated, consideration should be given to increasing the curve lengths to provide additional sight distance and reducing the length of the 5 percent grade. Using the curve lengths shown below, the 5 percent grade occurs at station 9+50 only, and reduces from that point in each direction.



Using equation 4.4-2 with the 500-foot crest length and solving for  $S$ , stopping sight and passing sight distances provided are 789.5 feet and 950 feet, respectively. Since both are influenced by the adjacent sag curve, graphical analysis shows that actual minimum sight distances provided are 825 feet  $SSD$  and 1080 feet  $PSD$ , meeting the criteria for 60 mph.

Since the sag curve is longer than the stopping sight distance provided, the minimum  $SSD$  provided can be found using equation 4.4-7, and is 670 feet whenever the vehicle and 1 degree rise in headlight are on the sag.

It is worth noting that the downgrade of the roadway during the braking operation is much lower than the 5 percent used to calculate required stopping sight distance for the sag curve. It varies from  $-3.65$  to  $-.9$  percent at the steepest point that  $SSD$  is at its minimum for the curve shown above. In this respect, using the  $SSD$  adjusted for grades is significantly more conservative when applied to sag curves compared to crest curves, and may warrant closer analysis for situations where site constraints or impacts limit curve length.

**Example 2-3: Combination of Vertical and Horizontal Curves****Given:** Horizontal curve data $PI = 50+00.00$  $\Delta = 27^{\circ}15'18''$  (RT) $R = 3,000$  feet $S = 4.0\%$ 

Design speed = 60 mph

Two-lane, two-way roadway with 12-foot travel lanes, 4-foot shoulders

Guardrail on the inside shoulder with face of rail at edge of shoulder

Guardrail post height = 32 inches

Symmetrical vertical curve data $G1 = +2.00\%$  $G2 = -2.50\%$ 

VPI elev. = 1,308.00'

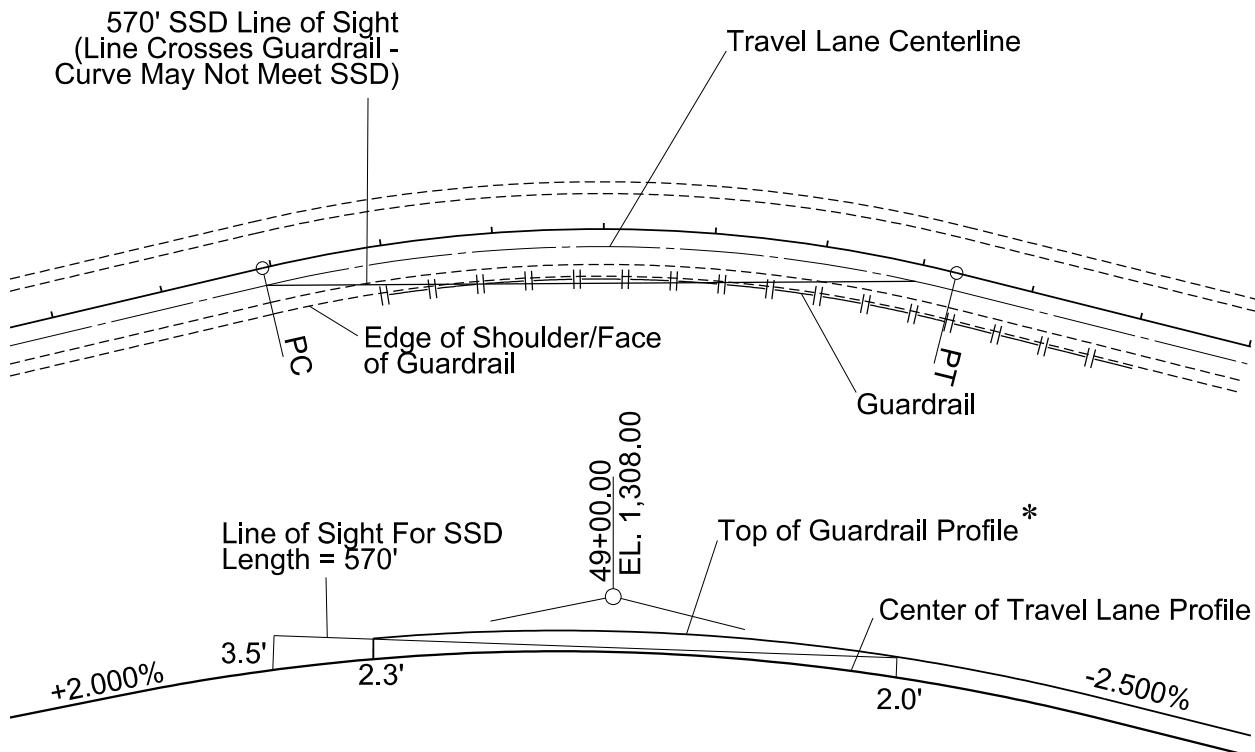
VPI station = 49+00.00

 $L = 2,000'$ **Problem:** Graphically determine if the combination of horizontal and vertical curves provides Stopping Sight Distance (SSD) using CAD software.**Solution:**

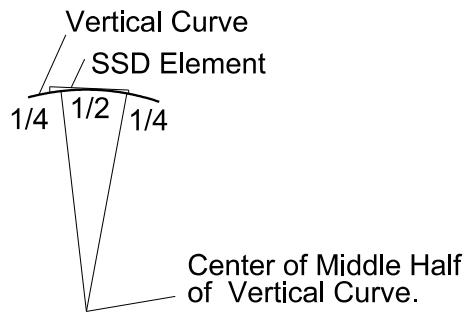
1. Draw the horizontal curve showing travel lanes, center of travel lanes, shoulders and guardrail.
2. Determine SSD for 60 mph from table in Exhibit 2-1. ( $SSD = 570'$ )
3. Draw a sight line the length of the SSD as a chord across the curve from the center of near travel lane to the center of near travel lane. If the line crosses the guardrail the curve may not meet SSD.
4. If the horizontal curve appears to provide a SSD line of sight, check the vertical profile for meeting SSD (step 5). If it appears that the curve does not meet the SSD, then graphically check the roadway profile with the guardrail profile shown to determine if the line of sight clears the top of the guardrail (step 6).
5. To graphically check the SSD of the roadway profile:
  - a. Draw the profile for the area of the horizontal curve which in this case includes a crest vertical curve.
  - b. Draw an element, to the same scale the profile was drawn, representing the SSD.
  - c. Draw the element with a horizontal line of sight line the length of the SSD and with a vertical leg under each end, 3.5' high on the driver's eye height side and 2.0' high on the object height side.
  - d. Place the element on the profile with the legs touching the profile.
  - e. Move the element along the profile through the vertical curve while keeping the legs on the profile.
  - f. If at any point the profile line crosses the line of sight part of the element, the curve does not meet SSD.

6. To graphically check the *SSD* on the roadway profile with the guardrail, draw the profile for the area of the horizontal curve which in this case includes a crest vertical curve. Draw the top of guardrail profile at the correct height above the roadway profile.
  - a. The guardrail profile elevation = roadway profile elevation + (guardrail post height - (distance from the face of rail to the center of the travel lane x the roadway cross slope rate)).
  - b. Draw an element, to the same scale the profile was drawn, representing the *SSD*.
  - c. Draw the element with a horizontal line of sight line the length of the *SSD* and with a vertical leg under each end, 3.5' high on the driver's eye height side and 2.0' high on the object height side.
  - d. Place the element on the roadway profile with the legs touching the profile.
  - e. Move the element along the roadway profile through the vertical curve.
  - f. If at any point the guardrail profile line crosses the horizontal part of the element, the vertical curve does not meet *SSD*.

This method can be used to check *SSD* and passing sight distance (*PSD*) on any combination of horizontal/vertical curves with possible sight restrictions caused by backslopes, rocks, fences, buildings, crops, etc. It can also be used to check *SSD* and *PSD* on multiple short vertical curves with little or no tangent grade between them.



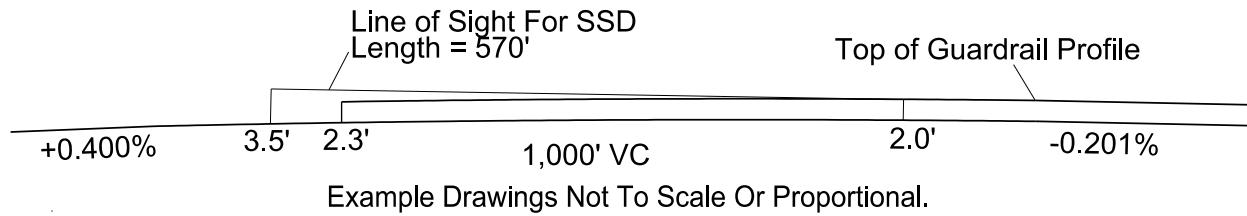
\* The guardrail profile elevation =  
 travel lane centerline profile elevation + [guardrail post height (2.7') - distance from the face of rail to the center of the travel lane (10') x the cross slope rate (0.4)] =  
 travel lane centerline profile elevation + [2.7' - (10' x 0.04) = 2.3']



To move the SSD element through the vertical curve, rotate the element about the center of middle half of the vertical curve. Some tweaking of the element may be required near the edges of the vertical curve.

The line of sight for the SSD is crossed by both the face of guardrail horizontal alignment and by the top of guardrail profile. Therefore, this combination of vertical curve, horizontal curve, and guardrail offset does not meet SSD. The design team may consider widening the shoulder, eliminating the roadside hazard that is requiring guardrail, using a larger radius horizontal curve, flattening the grades, and/or using a longer vertical curve. The exhibit shown below illustrates an example of modifications required of

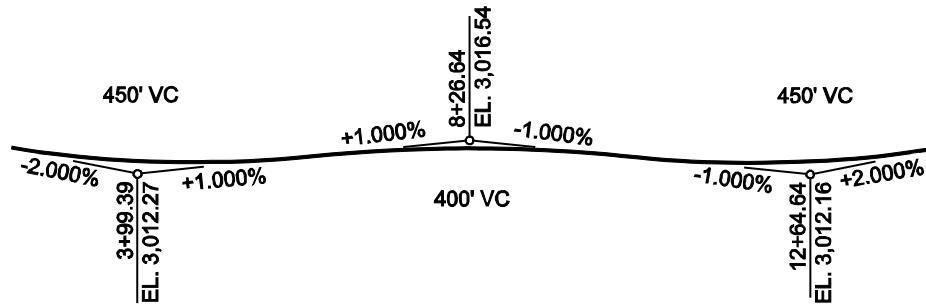
the profile to meet the *SSD*. It appears that increasing the horizontal curve radius or increasing the shoulder width/guardrail offset may be more practical ways to achieve the required *SSD* in this case.



### Example 2-4: Passing Sight Distance

**Given:** Refer to the below crest vertical curve for given information.

**Problem:** For a design speed of 60 mph on a rural, two-lane, two-way highway, does the following crest vertical curve meet minimum passing sight distance (*PSD*)? Give consideration to the multiple curves.



#### Solution:

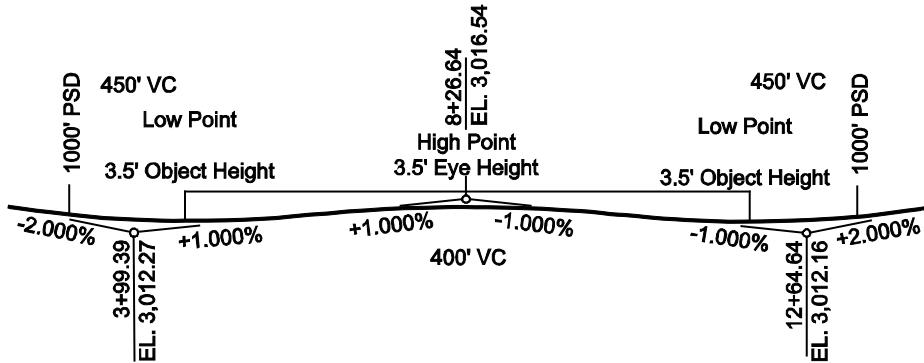
1. From Exhibit 2-10, the minimum passing sight distance for a design speed of 60 mph for the above crest vertical curve is 1,000'. Using the passing sight distance of 1,000' to calculate the length of vertical curve when *S* is greater than *L*, use Equation 4.4-2:

$$L = 2S - \frac{200 \times (\sqrt{h_1} + \sqrt{h_2})^2}{A}$$

The length of vertical curve required would be 600'. From inspection, the crest vertical curve (*Length* = 400') is less than the minimum required crest vertical curve (*Length* = 600') when designing for passing sight distance. If this crest vertical curve was connected by lengthy tangents sections extending at +1.0% and -1.0%, instead of short tangent sections connecting to

sag vertical curves as shown above, then this crest vertical curve would not meet the minimum passing sight distance for 60 mph design speed.

Consideration must be given for passing sight distance across multiple curves when they are connected by short tangents. If you plot the height of eye (3.5') at the high point of the crest vertical curve and the height of object (3.5') at the low point of both sag vertical curves, you can graphically determine if this crest vertical curve meets minimum passing sight distance.



Refer to the above diagram for plotting sight distance across the crest vertical curve. Plotting the low points of both sag vertical curves (at 3.5 foot object height) and the high point of the crest vertical curve (at 3.5 foot eye height), you can visually see that the sight distance is sufficient. If passing sight distance is sufficient at the low points, then it will also be sufficient at 1,000 feet.

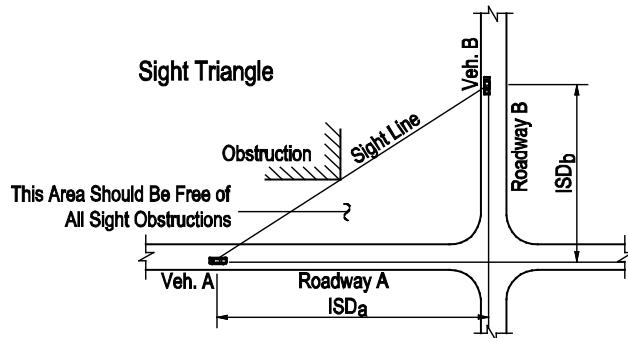
In conclusion, the crest vertical curve does meet the minimum requirements for 1,000 feet passing sight distance. If consideration was not given to passing sight distance across multiple curves, then this crest vertical curve would not have met the minimum passing sight distance.

**Example 2-5: Intersection Sight Distance (ISD) – No Traffic Control****Given:** No traffic control intersection.

Design speed: 35 mph (Roadway A)

Design speed: 25 mph (Roadway B)

Note: This exhibit is not applicable for State highways.



Design Speed (mph)	15	20	25	30	35	40	45	50
*Intersection Sight Distance (ft)	70	90	115	140	165	195	220	245

Note: For approach grades greater than 3%, multiply the sight distance values in this table by the appropriate adjustment factor from Appendix F, Exhibit F-8. The grade adjustment is based on the approach roadway grade only.

**Problem:** Determine legs of sight triangle.**Solution:** From the table shown above:

$$ISD_a = 165'$$

$$ISD_b = 115'$$

**Example 2-6: Intersection Sight Distance – Stop Controlled**

**Given:** Minor road intersects a 4-lane highway with a two-way, left-turn lane (TWLTL).  
Minor road is stop controlled.  
Design speed of the major highway is 50 mph.  
All travel lane widths are 12 feet.  
The TWLTL width is 14 feet.  
Trucks are not a concern.

**Problem:** Determine the intersection sight distance (*ISD*) to the left and right from the minor road.

**Solution:** The following steps will apply:

1. For the vehicle turning right from the minor road, the intersection sight distance (*ISD*) to the left can be determined directly from Appendix F, Exhibit F-12. For the 50-mph design speed, the *ISD* to the left is 480 feet.
2. For the vehicle turning left, the *ISD* must reflect the additional time required to cross the additional lanes. The following will apply:
  - a. First, determine the extra width required by the one additional travel lane and the TWLTL and divide this number by 12 feet:

$$(12 + 14) \div 12 = 2.2 \text{ lanes}$$

- b. Next, multiply the number of lanes by 0.5 seconds to determine the additional time required:

$$(2.2 \text{ lanes}) \times (0.5 \text{ sec/lane}) = 1.1 \text{ seconds}$$

- c. Add the additional time to the basic gap time of 7.5 seconds and insert this value into Appendix F, Equation F.3-1:

$$ISD = (1.47) \times (50) \times (7.5 + 1.1) = 632'$$

Provide an *ISD* of 632' to the right for the left-turning vehicle.

3. Check the crossing vehicle, as discussed in Appendix F, Section F.3.2.2. The following will apply:
  - a. First determine the extra width required by the two additional travel lanes and the TWLTL and divide this number by 12 feet:

$$\frac{(12 + 12 + 14)}{12} = 3.2 \text{ lanes}$$

b. Next, multiply the number of lanes by 0.5 seconds to determine the additional time required:

$$(3.2 \text{ lanes})(0.5 \text{ sec/lane}) = 1.6 \text{ seconds}$$

c. Add the additional time to the basic gap time of 6.5 seconds and insert this value into Appendix F, Equation F.3-1:

$$ISD = (1.47) (50) (6.5 + 1.6) = 595'$$

The 595' for the crossing maneuver is less than the 635' required for the left-turning vehicle and, therefore, is not the critical maneuver.

### Example 2-7: Decision Sight Distance

**Given:** A rural two-lane, two-way, level roadway with a design speed of 60 mph.

**Problem:** Determine the associated avoidance maneuvers for the given roadway and determine the decision sight distances for each of the avoidance maneuvers.

**Solution:** From the footnotes of Exhibit 2-12: This is a rural facility, the two avoidance maneuvers that address rural roads are A and C.

From Exhibit 2-12: Using the design speed of 60 mph, the decision sight distances for a rural roadway are:

Avoidance Maneuver A: 610 feet

Avoidance Maneuver C: 990 feet

# Horizontal Alignment Example Calculations

## Example 3-1: Spiral Curve

**Given:** Rural Two-Lane, Two-Way Highway

Design Speed = 70 mph

$\Delta = 15^{\circ}00'00''$

(Master) PI Station = 243+18.72

$R_c = 3,000$  feet

$e_{max} = 8\%$

Refer to Appendix H.1.1 for a diagram of the different elements of a spiral curve and Appendix H.1.2 for the associated definitions for these different elements.

**Problem:** If a spiral curve is warranted, determine the curve data for the spiral curve.

**Solution:** The following steps apply:

1. From Chapter 3, Section 3.2.1, a spiral curve is warranted on a rural State highway where the superelevation,  $e$ , is greater than or equal to 7%. From Chapter 3, Exhibit 3-5,  $e$  is 7% for  $V = 70$  mph and  $R_c = 3,000$  feet, therefore, use a spiral curve.
2. The length of the spiral curve ( $L_s$ ) is set equal to the superelevation runoff ( $L$ ) length. From Chapter 3, Exhibit 3-5,  $L = 210'$  for  $V = 70$  mph and  $R = 3,000$  feet, therefore,  $L_s = 210$  feet.
3. Calculate the curve parameters by using the spiral curve formulas provided in Appendix H.1.3:
  1.  $\theta_s = (L_s / R_c)(90 / \pi) = (210 / 3000)(90 / \pi)$   
 $\theta_s = 2.00535\dots^\circ$   
 $\theta_s = 2^{\circ}00'19''$  (rounded value)
  2.  $\Delta_c = \Delta - 2\theta_s = (15^{\circ}00'00'') - 2(2^{\circ}00'19'')$   
 $\Delta_c = 10^{\circ}59'22'' = 10.9894\dots^\circ$   
 (Note: Rounding to the nearest second requires decimal degrees to the nearest 0.0001.)
  3.  $L_c = \frac{\Delta_c}{360} 2\pi$     $R_c = \frac{10.9894}{360} (2\pi)(3000)$   
 $L_c = 575.4049\dots'$   
 $L_c = 575.40'$  (rounded value)
  4.  $T_s = (R_c + p) \tan(\Delta / 2) + k$
  5.  $E_s = (R_c + p) \left( \frac{1}{\cos \Delta / 2} - 1 \right) + p$

6. *Route Location and Design*, Hickerson provides two methods for determining  $p$  and  $k$  transition spiral values. The formula method from Hickerson's *Route Location and Design* pg. 375 is shown below;

$$p = L_s [0.00145444 \theta_s - 1.582315 \theta_s^3 (10)^{-8} + 1.022426 \theta_s^5 (10)^{-13} \dots]$$

$$k = L_s [0.5 - 5.076957 \theta_s^2 (10)^{-6} + 4.295915 \theta_s^4 (10)^{-11} \dots]$$

Calculating using these formulas and the length of spiral and theta calculated above:

$$p = 0.612' \text{ and } k = 104.996'$$

Hickerson's *Route Location and Design* also provides Functions of Unit Spiral Length Tables for interpolating unit values  $p_{\text{unit}}$  and  $k_{\text{unit}}$ . These are calculated by setting  $L_s$  equal to 1, and tabulated for integer values of  $\theta_s$ . Interpolating from the table  $p_{\text{unit}} = 0.002917$  and  $k_{\text{unit}} = 0.49998$ .

The values above are for a unit spiral length and need to be adjusted for  $L_s$ . Multiply the unit values by  $L_s$  to obtain the actual values for  $p$  and  $k$ .

$$p = p_{\text{unit}} (L_s) = (0.002917) (210) = 0.612473' \text{ rounding } p = 0.612'$$

$$k = k_{\text{unit}} (L_s) = (0.49998) (210) = 104.995713' \text{ rounding } k = 104.996'$$

Therefore:

$$T_s = (3000 + 0.612) \tan (15/2) + 104.996'$$

$$T_s = 500.034'$$

$$T_s = 500.03' \text{ (rounded value)}$$

$$E_s = (3000 + 0.612) (1/\cos(15/2) - 1) + 0.612'$$

$$E_s = 26.504'$$

$$E_s = 26.50' \text{ (rounded value)}$$

7. Determine the Stations for TS, SC, CS and ST:

$$\text{TS Station} = \text{PI Station} - T_s = [243+18.72] - 500.03' = 238+18.69$$

$$\text{SC Station} = \text{TS Station} + L_s = [238+18.69] + 210' = 240+28.69$$

$$\text{CS Station} = \text{SC Station} + L_c = [240+28.69] + 575.40' = 246+04.09$$

$$\text{ST Station} = \text{CS Station} + L_s = [246+04.09] + 210' = 248+14.09$$

## Example 3-2: Circular Curve

**Given:**  $\Delta = 7^\circ 00' 00''$

$R = 5,700$  feet

$e_{max} = 8\%$

PI Station = 154+56.42

Design Speed = 60 mph

Refer to Appendix H.2.1 for a diagram of the different elements of a circular curve and Appendix H.2.2 for the associated definitions for these different elements.

**Problem:** According to Chapter 3, Section 3.2.1 use a circular curve when the superelevation is less than 7%. From Chapter 3, Exhibit 3-5,  $e$  is 3% for  $V = 60$  mph and  $R = 5700'$ , therefore, use a circular curve. Calculate the curve parameters by using the circular curve formulas provided in Appendix H.2.3.

**Solution:** The following steps apply:

1. Calculate the Tangent Distance:

$$T = R(\tan(\Delta / 2)) = 5700(\tan(7 / 2))$$

$$T = 348.6269'$$

$$T = 348.63' \text{ (rounded value)}$$

2. Calculate the Length of Curve:

$$L = \frac{\Delta}{360} 2\pi R = \frac{7}{360} (2\pi)(5700)$$

$$L = 696.3863'$$

$$L = 696.39' \text{ (rounded value)}$$

3. Calculate the External Distance:

$$E = \frac{R}{\cos(\Delta/2)} - R = \frac{5700}{\cos(7/2)} - 5700$$

$$E = 10.6515'$$

$$E = 10.65' \text{ (rounded value)}$$

## 4. Length of Long Chord:

$$LC = 2R(\sin(\Delta / 2)) = (2)(5700)(\sin(7 / 2))$$

$$LC = 695.9533'$$

$$LC = 695.95' \text{ (rounded value)}$$

## 5. Calculate the Middle Ordinate:

$$M = R(1 - \cos(\Delta / 2)) = 5700(1 - \cos(7 / 2))$$

$$M = 10.6316'$$

$$M = 10.63' \text{ (rounded value)}$$

## 6. Stations are as follows:

$$\text{PC Station} = \text{PI Station} - T = [154+56.42] - 348.63' = 151+07.79$$

$$\text{PT Station} = \text{PC Station} + L = [151+07.79] + 696.39' = 158+04.18$$

### Example 3-3: Reverse Curve Superelevation Transition - Continuously Rotating Plane between Two Circular Curves

**Given:** A two-lane, two-way, rural roadway with a design speed of 45 mph and the following reverse curves (circular):

Curve 1	Curve 2
PI Station = 27+27.45	PI Station = 46+47.67
$\Delta = 73^\circ 08' 53''$ RT	$\Delta = 61^\circ 14' 40''$ LT
$R = 1,800$ feet	$R = 1,050$ feet
PC Station = 13+91.92	PC Station = 40+26.15
PT Station = 36+89.94	PT Station = 47+92.30

**Problem:** Calculate the reverse curve superelevation transition, assuming a continuously rotating plane, between the two circular curves.

**Solution:**

1. Determine if the curves meet the criteria for superelevation transition by the continuous rotating plane method.

From Chapter 3, Exhibit 3-5:

**Curve 1** requires a 5% superelevation ( $e1$ ), with 110' of Runoff ( $L1$ ), and 44' of Tangent Runout ( $TR1$ ) for normal superelevation development.

**Curve 2** requires a 7% superelevation ( $e2$ ), with 154' of Runoff ( $L2$ ), and 44' of Tangent Runout ( $TR2$ ) for normal superelevation development.

The tangent distance between the two curves is:

$$\text{PC2 Sta.} - \text{PT1 Sta.} = [40+26.15] - [36+89.94] = 336.21'$$

The distance outside of the curves required for normal superelevation development is 70% of the runoff for each curve + the runout distances. For these curves, normal superelevation transitions between the curves would require:

$$0.7 \times (L1 + L2) + TR1 + TR2 = 0.7 \times (110.00' + 154.00') + 2 \times 44' = 272.80'$$

The length of normal crown between transitions is  $336.21' - 272.80' = 63.41'$ . The  $TR$  distance for all superelevated curves with a design speed of 45 mph is 44'. The length of normal crown section provided (63.41') is less than twice the  $TR$  distance ( $2 \times 44' = 88'$ ) and therefore, it is not desirable to attain a normal crown section. The continuously rotating plane method is applicable in this situation.

Note that the minimum tangent distance between these two curves would be 70% of the two runoff distances, or 184.80'. Any tangent distance less than this would require either an increase in the normal transition rate or locating more of the transitions on the curves if the curves cannot be moved further away from each other. Either option requires approval of

the Highways Engineer as documented in the Alignment and Grade Review Report (AGR Report).

2. Locate the stations of full superelevation.

For continuous rotating plane transitions, the points of full superelevation are held and the transitions are combined into a continuous transition with a constant rate of change.

Points of full super elevation are determined normally, that is 30% of the standard runoff distances onto each curve.

The point where the superelevation starts to transition from 5% RT (point A on the exhibit below) is:

$$\text{Station A} = \text{PT1 station} - 0.3(L1) = [36+89.94] - 0.3 \times (110.00') = \text{Sta. } 36+56.94$$

The point where the transition ends at full 7% superelevation LT (point C on the exhibit below) is:

$$\text{Station C} = \text{PC2 station} + 0.3(L2) = [40+26.15] + 0.3 \times (154.00') = \text{Sta. } 40+72.35$$

3. Determine the location of level roadway (point B on the exhibit below).

The total length of continuous superelevation transition ( $L_{REV}$ ) is the distance between points A and C.

$$L_{REV} = \text{Station C} - \text{Station A} = [40+72.35] - [36+56.94] = 415.41'$$

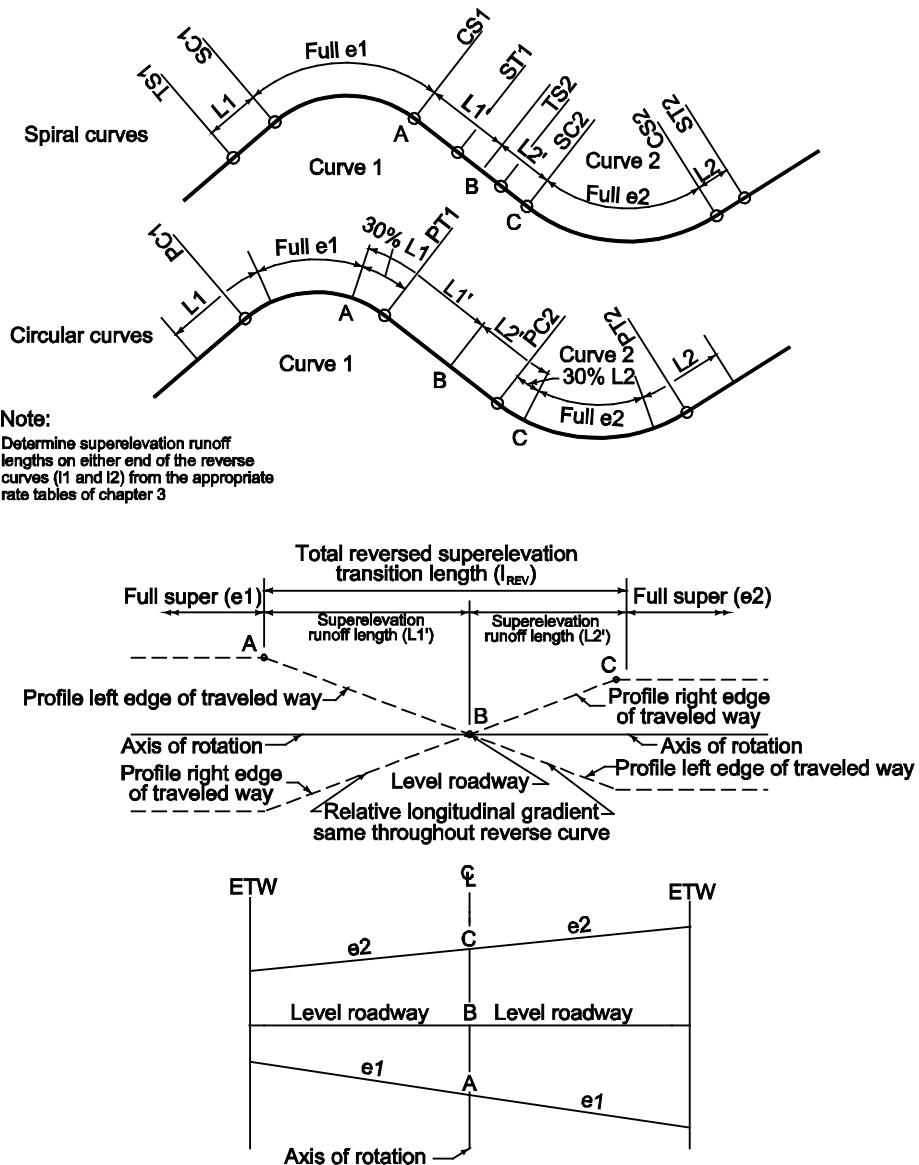
The length of superelevation transition from 5% RT to level ( $L1'$ ) is the distance between points A and B.

$$L1' = \frac{e1}{(e1+e2)} \times L_{REV} = \frac{5}{(5+7)} \times 415.41' = 173.09'$$

$$\text{Station B} = \text{Station A} + L1' = [\text{Station } 36+56.94] + 173.09 = 38+30.03$$

$L2'$  can either be determined by subtracting Station B from Station C, or from the following equation:

$$L2' = \frac{e2}{(e1+e2)} \times L_{REV} = \frac{7}{(5+7)} \times 415.41' = 242.32'$$



For checking the superelevation at a given station (point X) within the transition, identify whether the location is within  $L1'$  or  $L2'$ . If the station is less than Station B, it falls within  $L1'$ ; otherwise, it is within  $L2'$ .

$$e_x = \frac{\text{Station B} - \text{Station X}}{L1'} \times e1 \quad \text{or} \quad \frac{\text{Station X} - \text{Station B}}{L2'} \times e2$$

Determining the superelevation at a point can be useful in checking rollover and the effect of cross slope on approach turning movements, drainage or other cross slope critical criteria, and elevation/clearance for overhead structures.

In this example, if one wanted to determine the superelevation at Station 37+20.00:

37+20.00 is less than 38+30.03, therefore is located within the *L1'* section.

$$e = \frac{[38 + 30.03] - [37 + 20.00]}{173.09'} \times 5\% \text{ RT} = 3.18\% \text{ RT (rounded)}$$

### Example 3-4: Reverse Curve Superelevation Transition - Continuously Rotating Plane between Two Curves with Spiral Transitions

**Given:** A four-lane, two-way, open roadway with a design speed of 55 mph and the following reverse curves (w/ spiral transition):

Curve 1	Curve 2
PI Station = 314+76.54	PI Station = 323+93.50
$\Delta = 23^\circ 30' 00''$ LT	$\Delta = 21^\circ 18' 00''$ RT
R = 1,150 feet	R = 1,500 feet

**Problem:** Calculate the reverse curve superelevation transition, using a continuously rotating plane between the two curves with spiral transitions.

**Solution:**

1. Determine if the curves meet the criteria for superelevation transition by the continuous rotating plane method.

From Chapter 3, Exhibit 3-6:

**Curve 1** requires an 8% superelevation ( $e_1$ ), with 312' of Runoff ( $L_1$ ) which will coincide with the Spiral Transition ( $L_1 = L_{s1}$ ), and 78' of Tangent Runout ( $TR_1$ ) for normal superelevation development.

**Curve 2** requires a 7% superelevation ( $e_2$ ), with 273' of Runoff ( $L_2$ ) which will coincide with the Spiral Transition ( $L_2 = L_{s2}$ ), and 78' of Tangent Runout ( $TR_2$ ) for normal superelevation development.

Using spiral formulas found in Appendix H.1.3, the following parameters are calculated:

Curve 1	Curve 2
PI Station = 314+76.54	PI Station = 323+93.50
$\Delta = 23^\circ 30' 00''$ LT	$\Delta = 21^\circ 18' 00''$ RT
R = 1,150'	R = 1,500'
$L_s = 312'$	$L_s = 273'$
$\theta_s = 7^\circ 46' 20''$	$\theta_s = 5^\circ 12' 50''$
$p = 3.52464'$	$p = 2.06964'$
$k = 155.90436'$	$k = 136.46233'$
$T_s = 395.84'$	$T_s = 418.92'$
$\Delta_c = 7^\circ 57' 20''$	$\Delta_c = 10^\circ 52' 20''$
$L_c = 159.68'$	$L_c = 284.63'$
TS Station = 310+80.70	TS Station = 319+74.58
SC Station = 313+92.70	SC Station = 322+47.58
CS Station = 315+52.38	CS Station = 325+32.21
ST Station = 318+64.38	ST Station = 328+05.21

The tangent distance between the two curves is:

$$\text{TS2 Sta.} - \text{ST1 Sta.} = [319+74.58] - [318+64.38] = 110.20'$$

The distance outside of the curves required for normal superelevation development is the sum of the Tangent Runout distances:

$$TR1 + TR2 = 78.00' + 78.00' = 156.00'$$

The length of normal crown between transitions is  $110.20' - 156.00' = -45.80'$ . This distance is less than 2 times the TR length ( $2 \times 78' = 156'$ ), and the continuous rotating plane method is applicable in this situation.

2. Locate the stations of full superelevation.

For continuous rotating plane transitions, the points of full superelevation are held and the transitions are combined into a continuous transition with a constant rate of change.

The points of full superelevation are the SC and CS of each curve, with the entire circular curve section between these points at the full superelevation. The end of full 8% LT (point A on the exhibit below) is the CS of Curve 1, Station 315+52.38 and the SC of Curve 2, Station 322+47.58 is the beginning of full 7% super RT (point C on the exhibit below).

3. Determine the location of level roadway (point B on the exhibit below).

The total length of continuous superelevation transition ( $L_{REV}$ ) is the distance between points A and C.

$$L_{REV} = \text{Station C} - \text{Station A} = [322+47.58] - [315+52.38] = 695.20'$$

The length of superelevation transition from 8% LT to level ( $L1'$ ) is the distance between points A and B.

$$L1' = \frac{e1}{(e1+e2)} \times L_{REV} = \frac{8}{(8+7)} \times 695.20' = 370.77'$$

$$\text{Station B} = \text{Station A} + L1' = [315+52.38] + 370.77' = 319+23.15$$

This point is not identified in the plans specifically, except in the cross sections, but it indicates where the roadway surface drainage changes, and is helpful in determining the cross slope at any point within the transition. From 319+23.15 the roadway drains left to right back on station, and drains right to left ahead on station.

$L2'$  can be calculated similarly:

$$L2' = \frac{e2}{(e1+e2)} \times L_{REV} = \frac{7}{(8+7)} \times 695.20' = 324.43'$$

For checking the superelevation at a given station (point X) within the transition, identify whether the location is within  $L1'$  or  $L2'$ . If the station is less than Station B, it falls within  $L1'$ ; otherwise, it is within  $L2'$ .

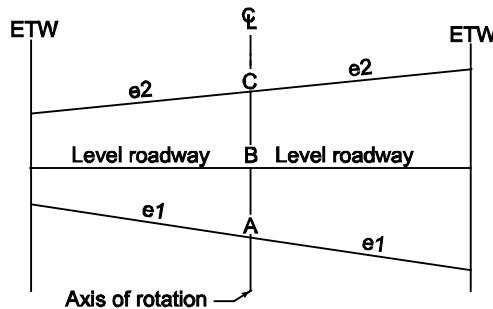
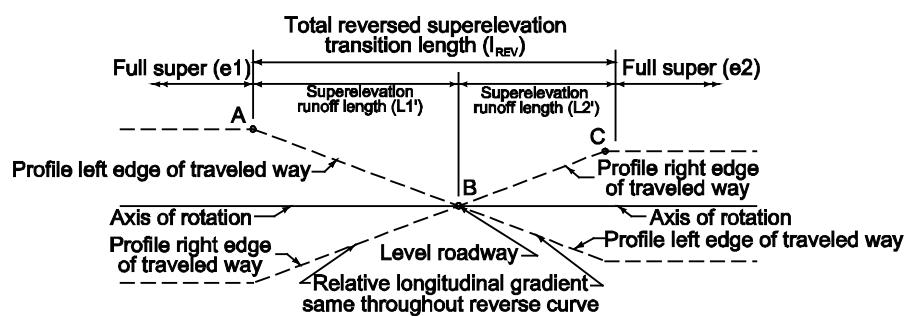
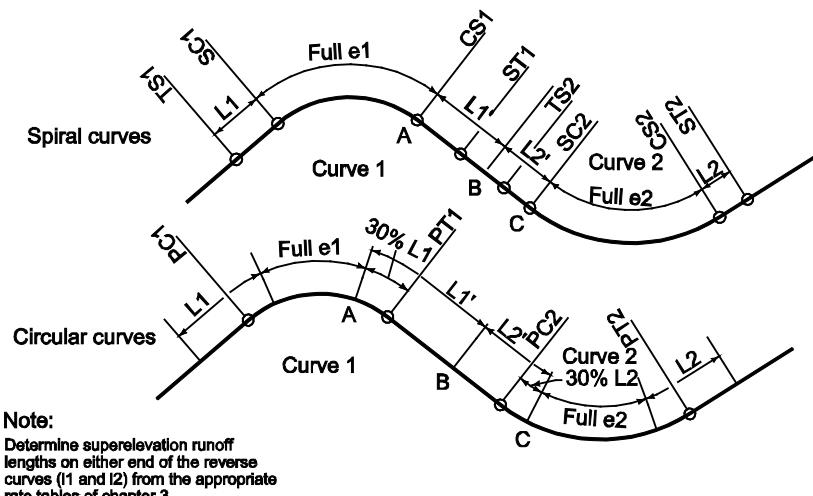
$$e_x = \frac{\text{Station B} - \text{Station X}}{L1'} \times e1 \quad \text{or} \quad \frac{\text{Station X} - \text{Station B}}{L2'} \times e2$$

Determining the superelevation at a point can be useful in checking rollover and the effect of cross slope on approach turning movements, drainage or other cross slope critical criteria, and elevation/clearance for overhead structures.

In this example, if one wanted to determine the superelevation at Station 321+00.00:

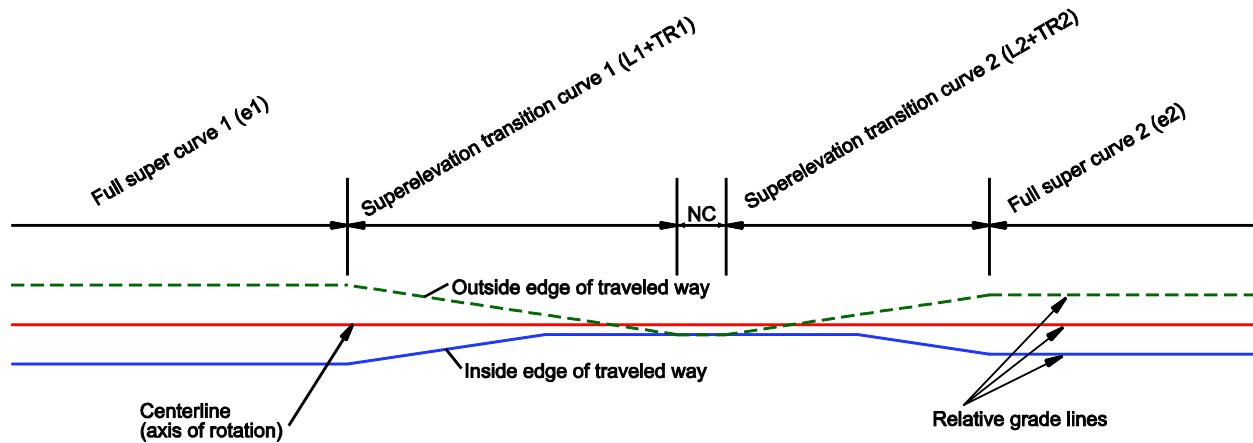
321+00.00 is greater than 319+23.15, therefore is located within the  $L2'$  section.

$$e = \frac{[321+00.00] - [319+23.15]}{324.43'} \times 7\% \quad \text{RT} = 3.82\% \text{ RT (rounded)}$$



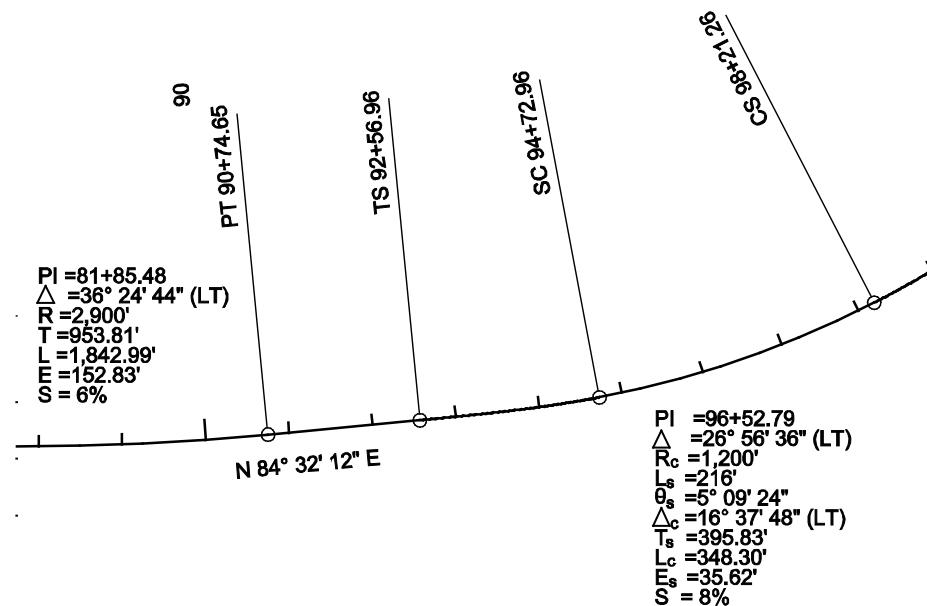
### Example 3-5: Broken Back Curve Application

**Given:** Superelevation transition for horizontal curves in the same direction (broken-back curves). The exhibit below represents the relative grade lines of each edge of the traveled way for a roadway transitioning through two superelevated curves in the same direction:



When the standard transition lengths result in a normal crown (NC) section between the curves less than 200 feet long, do not transition down to normal crown. Instead, transition down to a section with less superelevation, but not less than the normal crown cross slope that can be maintained for at least 200 feet.

**Problem:** Given the following alignment, determine the superelevation transition between the curves assuming a 60 mph design speed, two-lane, two-way roadway rotated about the centerline, and a normal crown of 2 percent:



**Solution:**

1. Determine the normal transition lengths and locations for each curve.

For a design speed of 60 mph, Exhibit 3-5 indicates that 27 feet of transition length is needed for each 1 percent change in cross slope.

The first curve is circular, with 6 percent superelevation. For circular curves, 30 percent of the runoff length is located on the curve:

$$\text{Start of transition (6\%)} = [\text{PT station}] - 0.3(L) = [90+74.65] - 0.3(162') = \text{Sta. } 90+26.05$$

$$\text{End of transition (NC)} = [90+26.05] + L + TR = [90+26.05] + 162' + 54' = \text{Sta. } 92+42.05$$

For the second curve, the 8 percent runoff length is applied through the corresponding spiral transition length (216 feet). The tangent runout distance (54 feet) back from the TS station is the station where normal crown would end, and the transition to 8 percent superelevation begins:

$$\text{Start of transition (NC)} = [\text{TS station}] - TR = [92+56.96] - 54' = \text{Sta. } 92+02.96$$

$$\text{End of transition (8\%)} = [\text{SC station}] = \text{Sta. } 94+72.96$$

2. Check the length of normal crown between transitions:

$$\text{Length of NC provided} = [92+02.96] - [92+42.05] = -39.09'$$

If the length of NC section provided is 200 feet or more, standard transitions may be provided. Otherwise, proceed on to Step 3. (A negative value, as in this case, indicates the distance that the transition locations overlap each other.)

3. Determine the intermediate rate of superelevation that can be held for at least 200 feet between transitions using the following equation:

$$S' = \frac{200' - \text{length of NC provided (feet)}}{2 \times \text{length for 1\% change (feet)}} - NC$$

where:

$S'$  = intermediate percent superelevation

NC = normal crown cross slope

$$S' = \frac{200' - (-39.09')}{2 \times 27'} - 2 = \frac{239.09'}{54'} - 2 = 2.43, \text{ round } \Rightarrow 3\%$$

Note: Round up to the next integer value equal to or greater than the normal crown cross slope (2% is typical for paved roadways).

4. Determine the stations within the transitions where the superelevation is 3 percent:

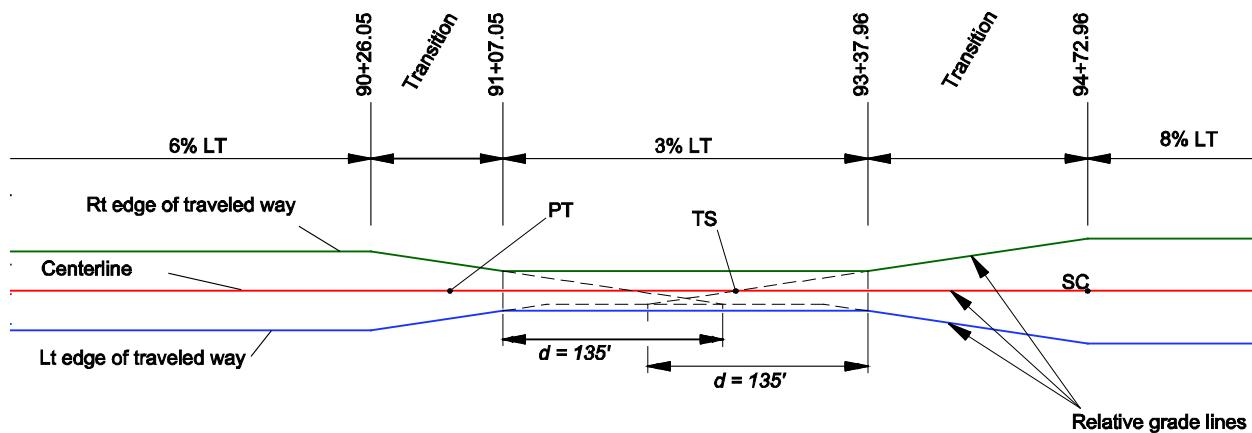
Working from the end of each transition where NC would be provided, the distance,  $d$ , to the 3 percent superelevated section is calculated:

$$d = (S' + NC) \times \text{length for 1\% change (feet)} = (3 + 2) \times 27' = 135'$$

Station of start of constant 3% = [92+42.05] - 135' = Sta. 91+07.05

Station of end of constant 3% = [92+02.96] + 135' = Sta. 93+37.96

The figure below represents the relative grade lines for the edge of traveled way for this example.



These transitions would be indicated in the plans by the stationing callouts on the superelevated typical section, rather than transitioning back and forth between typicals.

For example:

XX+XX.XX to 90+26.05	6% LT
90+26.05 to 91+07.05	Trans. 6% LT to 3% LT
91+07.05 to 93+37.96	3% LT
93+37.96 to 94+72.96	Trans. 3% LT to 8% LT
94+72.96 to YY+YY.YY	8% LT

## Example 3-6: Compound Curve Application

**Given:**  $\Delta = 40^\circ$

$R_1 = 600$  feet

$R_2 = 250$  feet

$p = 5'$

Refer to Appendix H.3.1 for a diagram of the different elements of a compound curve.

**Problem:** Determine the curve data for the compound curve.

**Solution:** Use the compound curve formulas from Appendix H.3.2 to calculate the curve parameters:

$$1. \quad T_1 = (R_2 + p) \tan(\Delta/2) = (250' + 5') \tan(40^\circ/2)$$

$$T_1 = 92.81'$$

$$2. \quad \Delta_1 = \cos^{-1} \left[ \frac{R_1 - R_2 - p}{R_1 - R_2} \right] = \cos^{-1} \left[ \frac{600' - 250' - 5'}{600' - 250'} \right]$$

$$\Delta_1 = 9.6963^\circ$$

$$\Delta_1 = 9^\circ 41' 47'' \text{ (rounded value)}$$

$$3. \quad T = T_1 + (R_1 - R_2) \sin \Delta_1 = 92.81' + (600' - 250') \sin(9.6963^\circ)$$

$$T = 151.7591'$$

$$T = 151.76' \text{ (rounded value)}$$

$$4. \quad T_2 = T_1 - R_2 \sin \Delta_1 = 92.81' - (250') \sin(9.6963^\circ)$$

$$T_2 = 50.7036'$$

$$T_2 = 50.70' \text{ (rounded value)}$$

$$5. \quad E = \frac{R_2 + p}{\cos(\Delta/2)} - R_2 = \frac{250' + 5'}{\cos(40^\circ/2)} - 250'$$

$$E = 21.3653'$$

$$E = 21.37' \text{ (rounded value)}$$

$$6. \quad M = R_2 - (R_2 \cos (\Delta / 2 - \Delta_1)) = 250' - \left( 250' \cos \left( \frac{40^\circ}{2} - 9.6963^\circ \right) \right)$$

$$M = 4.0316'$$

$$M = 4.03' \text{ (rounded value)}$$

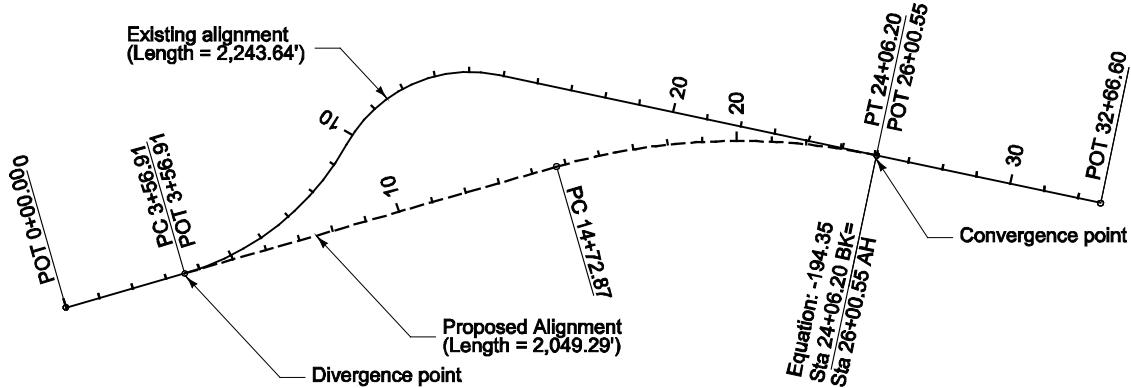
$$7. \quad y = (R_2 + p) - R_2 \cos \Delta_1 = (250' + 5') - (250') \cos(9.6963^\circ)$$

$$y = 8.5714'$$

$$y = 8.57' \text{ (rounded value)}$$

## Example 3-7: Station Equation Applications – Negative (Gap) Equation

**Given:** An existing compound curve is reconstructed with a proposed simplified alignment:



**Problem:** The proposed alignment reduces the overall length of the alignment, creating a stationing discrepancy at the end of the project. Determine a station equation to correct the stationing discrepancy.

**Solution:** Determine the negative (gap) station equation as follows:

1. Determine Back (BK) Station

$$\text{BK Sta.} = \text{Divergence Sta.} + \text{Proposed Alignment Length}$$

$$\text{BK Sta.} = [3+56.91] + 2,049.29'$$

$$\text{BK Sta.} = 24+06.20$$

2. Determine Ahead (AH) Station

$$\text{AH Sta.} = \text{Divergence Sta.} + \text{Existing Alignment Length}$$

$$\text{AH Sta.} = [3+56.91] + 2,243.64'$$

$$\text{AH Sta.} = 26+00.55$$

3. Determine Station Equation

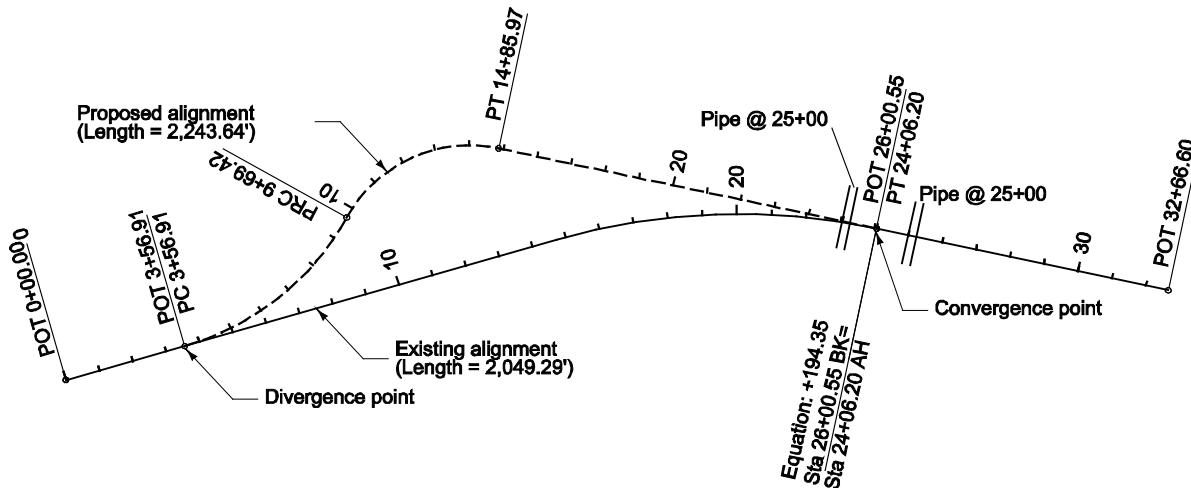
$$\text{Sta. Equation} = \text{BK Sta.} - \text{AH Sta.}$$

$$\text{Sta. Equation} = [24+06.20] - [26+00.55]$$

$$\text{Sta. Equation} = -194.35'$$

## Example 3-8: Station Equation Applications – Positive (Overlap) Equation

**Given:** An existing alignment is reconstructed with a proposed reverse curve:



**Problem:** The proposed alignment increases the overall length of the alignment, creating a stationing discrepancy at the end of the project. Determine a station equation to correct the stationing discrepancy.

**Solution:** Determine the positive (overlap) station equation as follows:

1. Determine Back (BK) Station

$$\text{BK Sta.} = \text{Divergence Sta.} + \text{Proposed Alignment Length}$$

$$\text{BK Sta.} = [3+56.91] + 2,243.64'$$

$$\text{BK Sta.} = 26+00.55$$

2. Determine Ahead (AH) Station

$$\text{AH Sta.} = \text{Divergence Sta.} + \text{Existing Alignment Length}$$

$$\text{AH Sta.} = [3+56.91] + 2,049.29'$$

$$\text{AH Sta.} = 24+06.20$$

3. Determine Station Equation

$$\text{Sta. Equation} = \text{BK Sta.} - \text{AH Sta.}$$

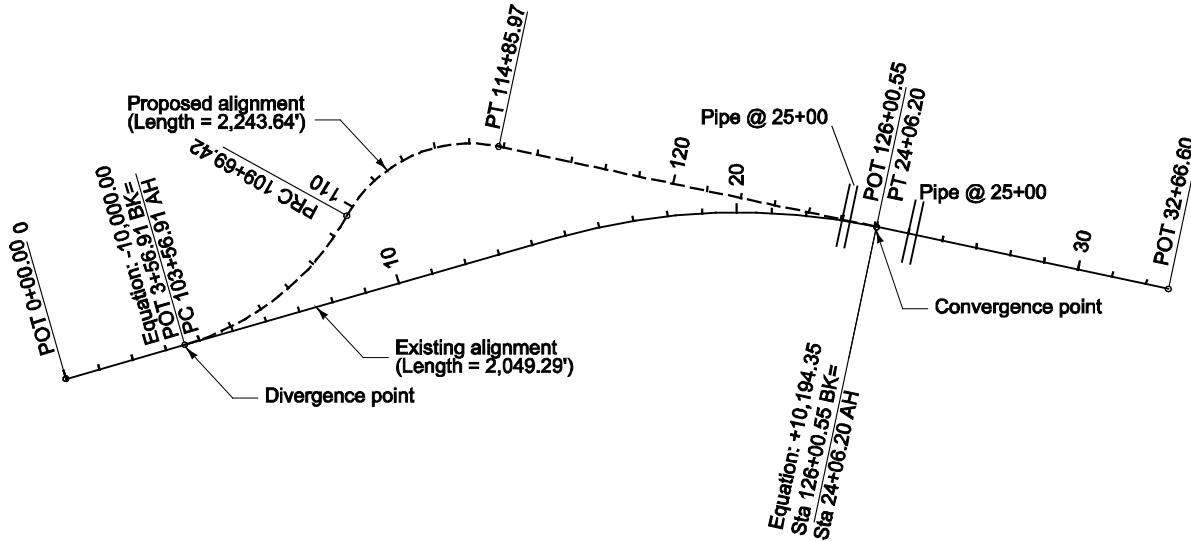
$$\text{Sta. Equation} = [26+00.55] - [24+06.20]$$

$$\text{Sta. Equation} = +194.35'$$

**Note:** This scenario can create an undesirable condition where project features can have coincident stations (see culverts in figure above for example). See the following example for a solution to this condition.

## Example 3-9: Station Equation Applications – Alternate Stationing

**Given:** An existing alignment is reconstructed with a proposed reverse curve:



**Problem:** The proposed alignment increases the overall length of the alignment, creating a stationing discrepancy at the end of the project. Determine alternate stationing for the proposed alignment to correct the stationing discrepancy and to avoid coincident stations.

**Solution:** Determine the alternate stationing and station equation as follows:

1. Establish Alternate Alignment Ahead (AH) Stationing at Divergence

$$\text{AH Sta.} = \text{Divergence BK Sta.} - \text{Sta. Equation}$$

$$\text{AH Sta.} = [3+56.91] - (-10,000.00')$$

$$\text{AH Sta.} = 103+56.91$$

2. Determine Back (BK) Station at Convergence

$$\text{BK Sta.} = \text{Divergence AH Sta.} + \text{Proposed Alignment Length}$$

$$\text{BK Sta.} = [103+56.91] + 2,243.64'$$

$$\text{BK Sta.} = 126+00.55$$

3. Determine Ahead (AH) Station at Convergence

$$\text{AH Sta.} = \text{Divergence BK Sta.} + \text{Existing Alignment Length}$$

$$\text{AH Sta.} = [3+56.91] + 2,049.29'$$

$$\text{AH Sta.} = 24+06.20$$

## 4. Determine Station Equation at Convergence

Sta. Equation = Convergence BK Sta. – Convergence AH Station

Sta. Equation = [126+00.55] – [24+06.20]

Sta. Equation = +10,194.35'

Note: This scenario corrects the undesirable condition where project features can have coincident stations (see culverts in figure above for example). See the previous example describing the undesirable condition.

# Vertical Alignment Example Calculations

## Example 4-1: Compute Elevations and Stations at Specific Points on a Symmetrical Sag Vertical Curve

**Given:**  $G_1 = -1.75\%$

$G_2 = +2.25\%$

Elevation of VPI = 577.43'

Station of VPI = 15+00

$L = 1,200'$

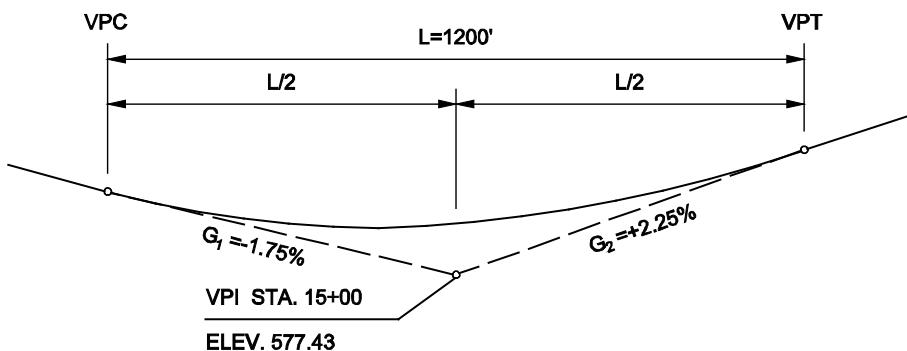
Symmetrical Vertical Curve

Refer to Appendix H.4.1 for a diagram of the different elements of a symmetrical vertical curve and Appendix H.4.2 for the associated definitions for these different elements.

**Problem:** Compute the vertical curve elevations for each 50-foot station. Compute the low point elevation and stationing.

**Solution:** The following steps apply:

1. Draw a diagram of the vertical curve and determine the station at the beginning (VPC) and the end (VPT) of the curve.



$$\text{VPC Station} = \text{VPI Sta.} - \frac{1}{2} L = [15+00] - (0.5)(1200') = 9+00$$

$$\text{VPT Station} = \text{VPI Sta.} + \frac{1}{2} L = [15+00] + (0.5)(1200') = 21+00$$

2. Use the symmetrical vertical curve formulas from Appendix H.4.3 to calculate the elements of the vertical curve:

$$CURVE\ ELEV. = TAN.\ ELEV. + Z$$

Where:

Left of VPI (X <sub>1</sub> measured from VPC):	Right of VPI (X <sub>2</sub> measured from VPT):
(a) $TAN\ ELEV. = VPC\ ELEV. + G_1 \left( \frac{X_1}{100} \right)$	(a) $TAN\ ELEV. = VPT\ ELEV. - G_2 \left( \frac{X_2}{100} \right)$
(b) $Z_1 = X_1^2 \frac{(G_2 - G_1)}{200L}$	(b) $Z_2 = X_2^2 \frac{(G_2 - G_1)}{200L}$

3. Set up a table to show the vertical curve elevations at the 50-foot stations, substituting the values into the above equations.

Station	Inf.	Tangent Elevation	X	X <sup>2</sup>	Z=X <sup>2</sup> /60,000 <sup>1</sup>	Grade Elevation
9+00	VPC	587.930	0	0	0	587.93
9+50		587.055	50	2,500	0.0417	587.10
10+00		586.180	100	10,000	0.1667	586.35
10+50		585.305	150	22,500	0.3750	585.68
11+00		584.430	200	40,000	0.6667	585.10
11+50		583.555	250	62,500	1.0417	584.60
12+00		582.680	300	90,000	1.5000	584.18
12+50		581.805	350	122,500	2.0417	583.85
13+00		580.930	400	160,000	2.6667	583.60
13+50		580.055	450	202,500	3.3750	583.43
14+00		579.180	500	250,000	4.1667	583.35
14+50		578.305	550	302,500	5.0417	583.35
15+00		577.430	600	360,000	6.0000	583.43
15+50		578.555	550	302,500	5.0417	583.60
16+00		579.680	500	250,000	4.1667	583.85
16+50		580.805	450	202,500	3.3750	584.18
17+00		581.930	400	160,000	2.6667	584.60
17+50		583.055	350	122,500	2.0417	585.10
18+00		584.180	300	90,000	1.5000	585.68
18+50		585.305	250	62,500	1.0417	586.35
19+00		586.430	200	40,000	0.6667	587.10
19+50		587.555	150	22,500	0.3750	587.93
20+00		588.680	100	10,000	0.1667	588.85
20+50		589.805	50	2,500	0.0417	589.85
21+00	VPT	590.930	0	0	0	590.93

<sup>1</sup> The 60,000 value is calculated according to  $200L/(G_2 - G_1) \rightarrow (200*1,200)/(2.25 - (-1.75)) = 60,000$ .

4. Calculate the low point on the curve:

$$\text{To determine distance " } X_T \text{ " from VPC: } X_T = \frac{LG_1}{G_1 - G_2}$$

$$X_T = \frac{LG_1}{G_1 - G_2} = \frac{1200'(-1.75)}{-1.75 - 2.25} = \frac{-2,100.00'}{-4.00} = 525.00' \text{ from VPC}$$

To determine low point stationing:  $VPC\ Sta. + X_T$

Therefore, the Station at the low point is:

$$VPC_{STA} + X_T = [9 + 00] + (525) = 14 + 25$$

To determine the low point elevation on the vertical curve:

$$ELEV_{LOW\ POINT} = ELEV\ VPC - \frac{LG_1^2}{(G_2 - G_1)200}$$

Elevation of the low point on the curve equals:

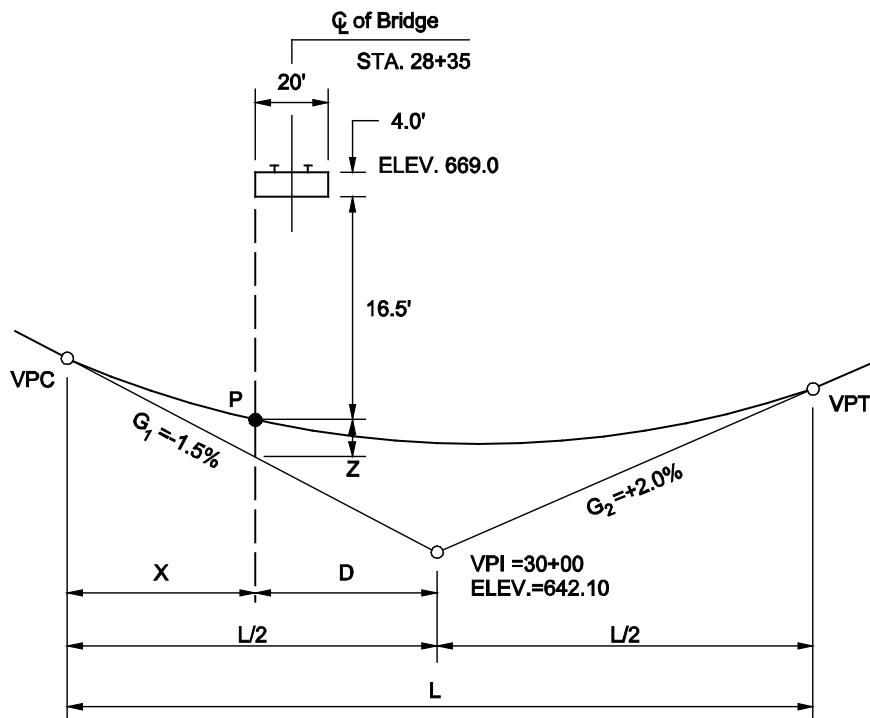
$$Elev.\ VPC - \frac{LG_1^2}{(G_2 - G_1)200} = 587.93' - \frac{1,200'(-1.75)^2}{(2.25 - (-1.75))200} = 583.34'$$

**Example 4-2: Symmetrical Vertical Curve Through a Fixed Point****Given:** Design Speed = 55 mph $G_1 = -1.5\%$  $G_2 = +2.0\%$ 

VPI Station = 30+00

VPI Elevation = 642.10'

Refer to Appendix H.4.1 for a diagram of the different elements of a symmetrical vertical curve and Appendix H.4.2 for the associated definitions for these different elements.

**Problem:** At Station 28+35, the new highway must pass under the center of an existing railroad which is at elevation 669.00' at the highway centerline. The railroad bridge that will be constructed over the highway will be 4.0' in depth, 20.0' in width and at right angles to the highway. What would be the length of the symmetrical vertical curve that would provide a 16.5' clearance under the railroad bridge?**Solution:**1. Sketch the problem with known information labeled.

2. Determine the station where the minimum 16.5' vertical clearance will occur (Point P):

From inspection of the sketch, the critical location appears to be on the left side of the railroad bridge. The critical station is:

$$STA. P = BRIDGE CENTERLINE STATION - \frac{1}{2} (BRIDGE WIDTH)$$

$$STA. P = [28 + 35] - \frac{20'}{2}$$

$$STA. P = 28 + 25$$

3. Determine the elevation of Point P:

$$ELEV. P = ELEV. TOP RAILROAD BRIDGE - BRIDGE DEPTH - CLEARANCE$$

$$ELEV. P = 669.00' - 4.00' - 16.50'$$

$$ELEV. P = 648.50'$$

4. Determine distance,  $D$ , from Point P to VPI:

$$\begin{aligned} D &= STA. VPI - STA. P \\ &= [30 + 00] - [28 + 25] \\ &= 175' \end{aligned}$$

5. Determine the tangent elevation at Point P:

$$\begin{aligned} TAN. ELEV. AT P &= ELEV. VPI - G_1 \left( \frac{D}{100} \right) \\ &= 642.10 - (-1.5) \left( \frac{175}{100} \right) \\ &= 644.73' \end{aligned}$$

6. Determine the vertical curve correction (Z) at Point P:

$$\begin{aligned} Z &= ELEV. P - TAN. ELEV. \\ &= 648.50' - 644.73' \\ &= 3.77' \end{aligned}$$

7. Solve for X using the following equation:

$$X = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

where:

$X$  = Horizontal Distance: Measured from the VPC (or VPT) to any point on the vertical curve (feet)

$a = A$  = Algebraic Difference in Grade: The difference between the two tangent grades ( $G_1-G_2$ ) (percent)

$b = Z$  = Tangent Offset: The vertical distance from the tangent line to any point on the vertical curve (feet)

$c = D \times Z$  = Product of  $D$  (distance from the VPI to the subject point, P) and  $Z$  (tangent offset) (square feet)

$$X = \frac{400Z \pm \sqrt{160,000Z^2 + 1,600ADZ}}{2A}$$

$$X = \frac{400(3.77) \pm \sqrt{160,000(3.77)^2 + 1,600(3.5)(175)(3.77)}}{2(3.5)}$$

$$X = 564.44' \quad \text{AND} \quad X = -133.58' \quad (\text{Disregard})$$

8. Using either of the following equations, solve for  $L$ :

$$X + D = L/2 \quad \text{or} \quad L = 2(X + D)$$

$$L = 2(X + D)$$

$$L = 2(564.44' + 175')$$

$$L = 1,478.88'$$

9. Check the critical point assumption from Step 2. Since the sketch is based on an assumed length of curve, the low point of the curve is also at an assumed location. In this example, the tangent grades of the curve are not “sketched” correctly. They indicate that the low point of the curve is on the right side of the VPI. In fact, the low point is on the left side of the VPI, as the magnitude of  $G_1$  is less than that of  $G_2$ .

Using the equation for finding the low point of the curve (see example 4-1):  $X_T = \frac{LG_1}{G_1 - G_2}$

$$X_T = \frac{LG_1}{G_1 - G_2} = \frac{1478.88'(-1.50)}{-1.50 - 2.00} = \frac{-2,218.32'}{-3.50} = 633.81' \text{ from VPC}$$

The station of the low point of the sag is 28+94.37, which is on the right side of the center of the railroad bridge station of 28+35.00. Therefore, the critical point assumption made in Step 2 is confirmed. Proceed to the next step.

Note: If the low point station had been on the left side of the bridge centerline, the length of curve required for clearance would need to be recalculated for the correct critical location on the right side of the bridge. Completing the sketch as accurately as possible for the known elements will lessen the likelihood of assuming the incorrect critical point, particularly for cases where the overhead structure is much wider.

10. Determine if the solution meets the desirable stopping sight distance for the 55 mph design speed. From Exhibit 4-5, the desirable K-value:

$$K=115$$

The algebraic difference in grades:

$$A = G_2 - G_1 = (+2.0) - (-1.5) = 3.5$$

From Equation 4.4-9, the minimum length of vertical curve which meets the desirable stopping sight distance:

$$\begin{aligned} L_{MIN} &= KA \\ &= (115) \times 3.5 \\ &= 402.5' \end{aligned}$$

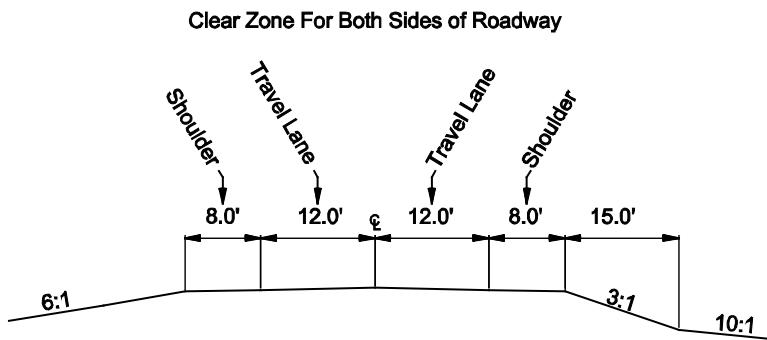
Therefore,  $L = 1,478.88'$  will provide the desirable stopping sight distance.

Note: This would be rounded down to 1,450' for recording on the plans.

# Roadside Safety Example Calculations

## Example 9-1: Clear Zone for Both Sides of the Roadway

**Given:** Design Speed = 55 mph  
 Annual Average Daily Traffic (AADT) = 4,750  
 Lane Width: 12 feet  
 Shoulder Width: 8 feet



**Problem:** Determine the clear zone distance for both sides of the roadway.

**Solution:** Using the procedure in Chapter 9, Section 9.2.2.2 for each side of the roadway:

1. For the left side of the roadway, the entire slope is flatter than 4:1, so the clear zone can be determined directly from Exhibit 9-1.

Left Clear Zone Width = 20 feet (Exhibit 9-1)

2. For the right side of the roadway, the 3:1 slope is non-recoverable. The procedure in Chapter 9, Section 9.2.2.2, Step 2 must be used.
3. Checking the recovery area beyond the toe, the slope of 10:1 is flatter than 4:1. This 10:1 slope is then used to determine the clear zone distance required from Exhibit 9-1.

Right Clear Zone Width = 20 feet (Exhibit 9-1)

4. The recovery area beyond the toe is calculated by subtracting the 8 feet of recoverable slope between the edge of traveled way and the hinge point from the 20 feet obtained in Step 3:

$$20' - 8' = 12' \text{ Distance beyond the toe}$$

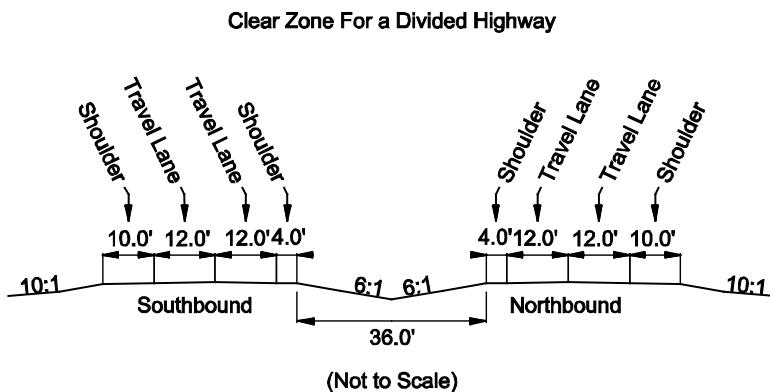
5. Since  $12' > 10'$ , 12' will be used as the recovery distance beyond the toe. (Chapter 9, Section 9.2.2.2, Step 2c)
6. Using the 12 feet recovery distance beyond the toe, the total clear zone width is calculated by summing the distance beyond the toe and the distance from the edge of traveled way to the toe:

$$8' + 15' + 12' = 35' \text{ Total Right Clear Zone Width}$$

**Example 9-2: Clear Zone for a Divided Highway**

**Given:**

- Design Speed: 70 mph
- AADT: 18,000
- Lane Width: 12 feet
- Outside Shoulder Width: 10 feet
- Inside Shoulder Width: 4 feet
- Median Width: 36 feet



**Problem:** Determine the clear zone distances.

**Solution:** Using the procedure in Chapter 9, Section 9.2.2.2 for each side of each roadway:

1. For the outside in each direction of travel, the slope is flatter than 4:1, so the clear zone can be determined directly from Exhibit 9-1:

Outside Clear Zone Width = 32 feet (Exhibit 9-1)

2. In the median, for the inside in each direction of travel, the inslope of 6:1 is flatter than 4:1, so a clear zone distance can be obtained from Exhibit 9-1:

Median Clear Zone Width = 32 feet (Exhibit 9-1)

3. The toe of the backslope is located at the center of the median which is 22 feet ( $4' + 18'$ ) from each inside edge of traveled way.

$22' < 32'$ , so the toe is within the clear zone.

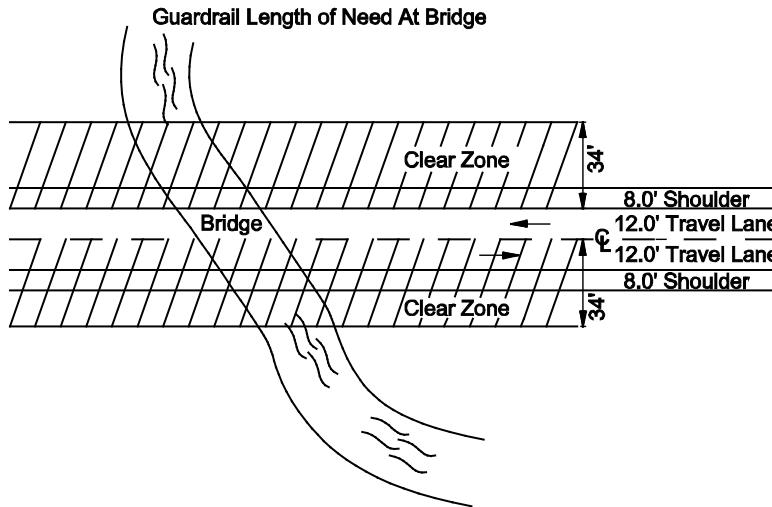
4. Since the toe is within the clear zone, the median toe must be checked for traversability. Using Exhibit 9-10, the median is determined to be traversable.

5. The percentage of the clear zone available up to the toe of the backslope is computed:  
 $22' \div 32' = 0.6875$
6. This value is subtracted from Step 2 and multiplied by the adjusted backslope clear zone factor of 30 feet obtained from Exhibit 9-6:  
 $(1 - 0.6875) \times 30' = 9.38'$  (Clear zone distance required beyond the toe)
7. The total clear zone is obtained by adding the value from Step 6 and the distance to the toe:  
 $9.38' + 22' = 31.38'$
8. This value is rounded up to the next foot, yielding a Total Median Clear Zone Width of 32 feet.

### Example 9-3: Guardrail Length of Need for Obstacle Extending Beyond the Clear Zone

**Given:**

- Design Speed: 55 mph
- AADT: 4,750
- Shoulder Width: 8 feet
- Lane Width: 12 feet
- Clear Zone Width: 34 feet
- Non-flared Guardrail (flared guardrail not allowed) with face of rail at edge of shoulder



**Problem:** Determine the length of need for guardrail on each side of the road on this end of the bridge (obstacle extends to the edge of the clear zone).

**Solution:**

1. Using Exhibit 9-16 the runout length is obtained by linear interpolation between 50 and 60 mph:

$$(160' + 210') \div 2 = 185'$$

2. A non-flared design will be used, Equation 9.4-2 is applied.

$$X = \frac{L_R(L_O - L_I)}{L_O}$$

- a. For a departure to the right:

$$L_R = 185 \text{ feet}$$

$$L_O = L_C = 34 \text{ feet}$$

$$L_I = 8 \text{ feet}$$

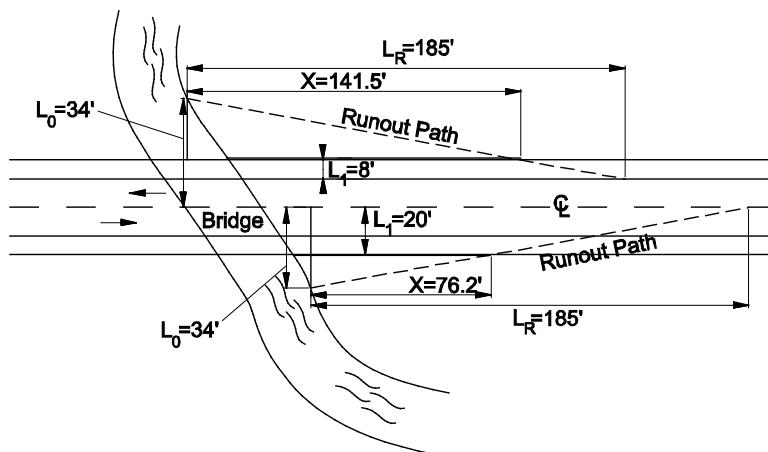
$$X = [185' \times (34' - 8')] \div 34' = 141.5' \text{ Length of Need}$$

b. For a departure to the left:

$$L_R = 185 \text{ feet}$$
$$L_0 = L_c = 34 \text{ feet}$$
$$L_1 = 12' + 8' = 20 \text{ feet}$$

$$X = [185' \times (34' - 20')] \div 34' = 76.2' \text{ Length of Need}$$

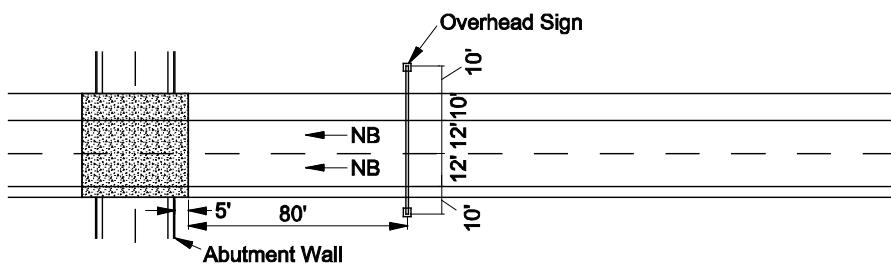
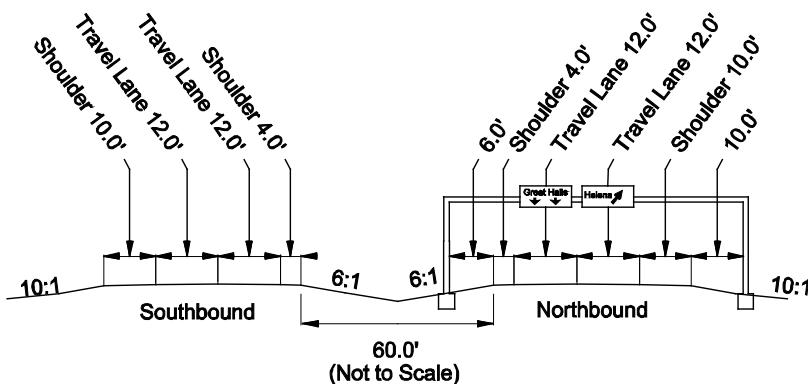
NOTE: Some of the length of need will be covered by terminal end sections and the bridge approach section. These lengths should be determined before computing the final length of rail required for each side.



**Example 9-4: Controlling Length of Need for Multiple Obstacles**

**Given:**

- Design Speed: 70 mph
- AADT: 18,000
- Outside Shoulder Width: 10 feet
- Inside Shoulder Width: 4 feet
- Lane Width: 12 feet
- Clear Zone Width: 32 feet
- Non-Flared Guardrail

**Guardrail Length of Need for Bridge and Overhead Sign**

**Problem:** Determine if the bridge or the sign controls the barrier length and find the length of need for guardrail on each side of the NB side of the highway.

**Solution:**

1. Using Exhibit 9-16 the runout length is determined to be 360 feet.
2. A non-flared design will be used. Equation 9.4-2 will be used to compute length of need.
3. For a left side departure:

- a. The length of need for the sign support is computed as follows:

$$L_R = 360 \text{ feet}$$

$$L_O = 4' + 6' = 10 \text{ feet (hazard is within the clear zone)}$$

$$L_I = 4 \text{ feet}$$

$$X = [360' \times (10' - 4')] \div 10' = 216.0' \text{ Length of Need}$$

- b. The length of need for the bridge abutment wall is computed as follows:

$$L_R = 360 \text{ feet}$$

$$L_O = L_C = 32 \text{ feet (hazard extends beyond the clear zone)}$$

$$L_I = 4 \text{ feet}$$

$$X = [360' \times (32' - 4')] \div 32' = 315.0' \text{ Length of Need}$$

- c. Guardrail must extend at least 315 feet from the abutment wall and 216 feet from the sign support. Adding 216 feet to the 85 feet from the abutment wall to the sign support gives 301 feet, which is less than 315 feet, so the bridge drop-off is the controlling feature and the final length of need is 315 feet from the abutment wall.

4. For a right side departure:

- a. The length of need for the sign support is computed as follows:

$$L_R = 360 \text{ feet}$$

$$L_O = 10' + 10' = 20 \text{ feet}$$

$$L_I = 10 \text{ feet}$$

$$X = [360' \times (20' - 10')] \div 20' = 180.0' \text{ Length of Need}$$

- b. The length of need for the bridge abutment wall is computed as follows:

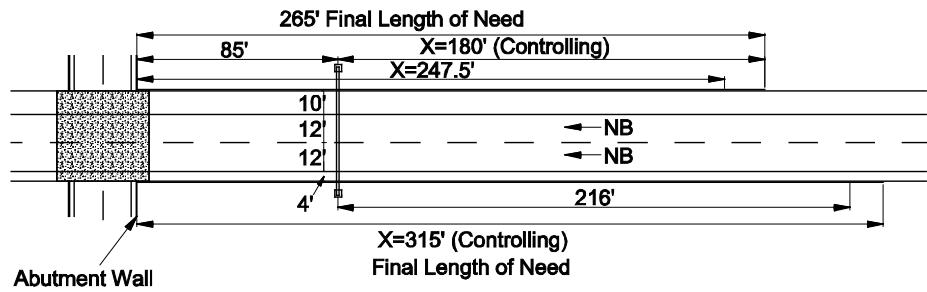
$$L_R = 360 \text{ feet}$$

$$L_O = L_C = 32 \text{ feet (hazard extends beyond the clear zone)}$$

$$L_I = 10 \text{ feet}$$

$$X = [360' \times (32' - 10')] \div 32' = 247.5' \text{ Length of Need}$$

c. Guardrail must extend at least 247.5 feet from the abutment wall and 180 feet from the sign support. Adding 180 feet to the 85 feet from the abutment wall to the sign support gives 265 feet, which is greater than 247.5 feet, so the sign is the controlling feature and the final length of need is 265 feet from the abutment wall.



### Example 9-5: Minimum Length of Culvert

**Background:** The length of large culverts with concrete edge protection must be long enough so that the top portion of concrete edge protection is out of the clear zone. This is typically straightforward on culverts that are perpendicular to the roadway. However, when drawing culverts on a skew, make sure that the skewed corners of the concrete edge protection are out of the clear zone.

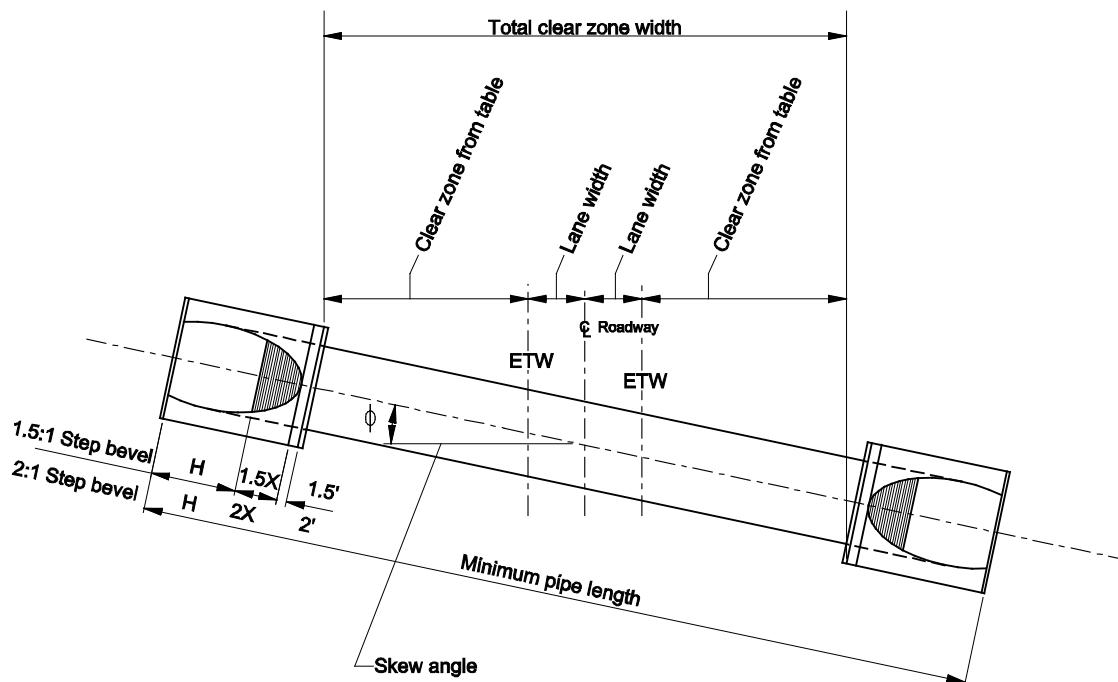
Use the following formulas to calculate the minimum lengths of skewed culverts to ensure that the concrete edge protection is out of the clear zone:

1.5:1 Step Bevel Formula:

$$\frac{(\sin \phi (0.5D + 4') \times 2 + \text{Total Clear Zone Width})}{\cos \phi} + (1.5' + 1.5X + H) \times 2 = \text{min. pipe length}$$

2:1 Step Bevel Formula:

$$\frac{(\sin \phi (0.5D + 4') \times 2 + \text{Total Clear Zone Width})}{\cos \phi} + (2' + 2X + H) \times 2 = \text{min. pipe length}$$



**Given:** 18' Diameter Circular Metal Pipe  
 $\phi = 12$  degree skew  
 2:1 Step Bevel Ends with Concrete Edge Protection on Inlet and Outlet  
 Clear Zone Distance from ETW = 36'  
 2 lane roadway with 12' lanes  
 Culvert Dimensions from Detailed Drawings:

$$D = 18'$$

$$X = 4.5'$$

$$H = 18'$$

**Problem:** Determine the minimum overall length of culvert to make sure that the concrete edge protection is out of the clear zone.

**Solution:**

2:1 Step Bevel Formula:

$$\frac{(\sin \phi (0.5D + 4') \times 2 + \text{Total Clear Zone Width})}{\cos \phi} + (2' + 2X + H) \times 2 = \text{min. pipe length}$$

$$\frac{(\sin 12^\circ ((0.5 \times 18') + 4') \times 2 + (36' + 12' + 12' + 36'))}{\cos 12^\circ} + (2' + (2 \times 4.5') + 18') \times 2 = \text{min. pipe length}$$

$$\frac{(0.2079 \times 13') \times 2 + 96'}{0.9781} + (29' \times 2) = \text{min. pipe length}$$

$$\frac{101.4054'}{0.9781} + 58' = \text{min. pipe length}$$

$$= 161.68', \text{ round to } 162'$$

# Quantity Summaries Example Calculations

## SYMMETRICAL SECTIONS BACKGROUND

Section 13.5.1.1 provides an overview of symmetrical sections that is the most commonly used typical section for determining the horizontal dimensions of various surface courses. The first step is to establish the width of subgrade using the following equation:

$$W_s = W_f + \left( \frac{tZ}{1 - CZ} \right)$$

where:

$W_s$  = half width of subgrade, feet

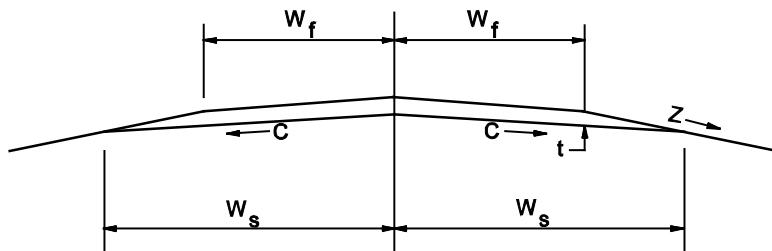
$W_f$  = half width of finished grade, feet

$t$  = total surfacing thickness at finished shoulder, feet

$Z$  = numerator of side slope ratio

(e.g.,  $Z = 6$  for a 6:1 side slope)

$C$  = crown, feet/feet (e.g., 0.02 for 2% cross slope)



Round the computed value for  $W_s$  to the nearest 0.1'. Because of the rounding process, the side slope through the surfacing courses will not be exactly 6:1, but the difference is negligible.

The second step is to establish the width of the intermediate surfacing courses. Compute each horizontal course dimension proportionately to its thickness. The width at the top of any surfacing course is determined by using the following equation:

$$W_X = W_f + \left[ \frac{(W_S - W_f)}{t} \right] t_X$$

where:

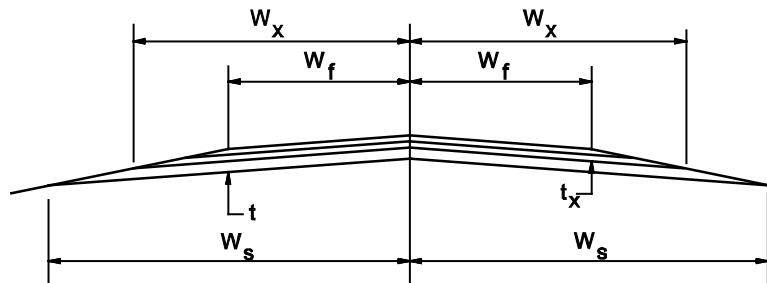
$W_X$  = half width of top of intermediate surfacing course, feet

$W_f$  = half width of finished grade, feet

$W_S$  = half width of subgrade, feet

$t$  = total surfacing thickness at finished shoulder, feet

$t_X$  = cumulative thickness of courses above  $W_X$  at finished shoulder, feet



Round the computed value for  $W_X$  to the nearest 0.1'.

**Example 13-1: Symmetrical Sections – Width of Subgrade**

**Given:**  $W_f = 20.0$  feet

$t = 1.80$  feet

$Z = 6:1$

$C = 0.02$

**Problem:** Determine the half width of subgrade.

**Solution:**

1. Use the following equation and solve for  $W_s$ .

$$W_s = W_f + \left( \frac{tZ}{1 - CZ} \right)$$

$$W_s = 20.0' + \frac{(1.8')(6)}{1 - (0.02)(6)}$$

$$W_s = 20.0' + 12.27' = 32.27'$$

$$W_s = 32.3' \text{ (Rounded to nearest 0.1 foot)}$$

The second step is to establish the width of the intermediate surfacing courses, which is shown in more detail in Example 13-2.

**Example 13-2: Symmetrical Sections – Intermediate Surface Width**

**Given:**  $t_x = 0.80'$

**Problem:** Using the values given in Example 13-1, determine the intermediate surfacing course half width.

**Solution:**

1. Use the following equation and solve for  $W_x$ .

$$W_x = W_f + \left[ \frac{(W_s - W_f)}{t} \right] t_x$$

$$W_x = 20.0' + \left[ \frac{(32.3' - 20.0')}{1.8'} \right] 0.80'$$

$$W_x = 20.0' + 5.467' = 25.467'$$

$$W_x = 25.5' \text{ (Rounded to nearest 0.1')}$$

## UNSYMMETRICAL SECTIONS BACKGROUND

Section 13.5.1.2 provides an overview of unsymmetrical sections that compute and record the widths to the left and right of centerline separately for determining the horizontal dimensions of various surface courses.

### Superelevated Sections.

To compute subgrade widths for superelevated sections, use the equations shown below:

#### Low Side

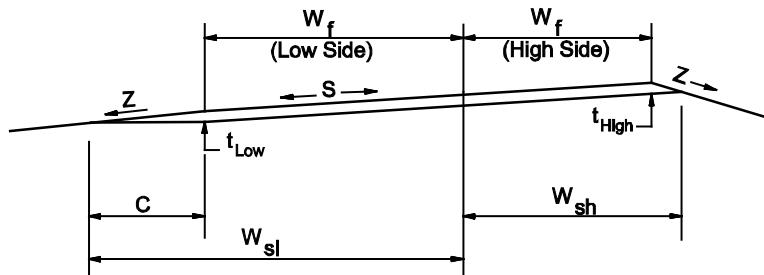
$$W_{sl} = W_f + \frac{tZ}{1 - CZ}$$

#### High Side

$$W_{sh} = W_f + \frac{tZ}{1 + SZ}$$

where:

- $W_{sl}$  = width from centerline to edge of subgrade on low side of superelevation, feet
- $W_{sh}$  = width from centerline to edge of subgrade on high side of superelevation, feet
- $W_f$  = width from centerline of finished grade, low or high side, feet
- $t$  = total thickness of surfacing at finished shoulder, feet
- $S$  = slope of superelevation, feet/feet (e.g., 0.07 for 7% superelevation)
- $Z$  = numerator of side slope ratio (e.g.,  $Z = "6"$  for a 6:1 side slope)
- $C$  = cross slope of tangent typical section, feet/feet (e.g., 0.02 for 2% cross slope)



Round each computed value for  $W_{sl}$  and  $W_{sh}$  to the nearest 0.1'.

### Divided Highways.

For both tangent and curved sections of divided highways, compute the subgrade widths left and right of centerline as follows:

**Tangent**

$$W_s(\text{median}) = W_f(\text{median}) + \frac{tZ}{1 - CZ}$$

$$W_s(\text{outside}) = W_f(\text{outside}) + \frac{tZ}{1 - CZ}$$

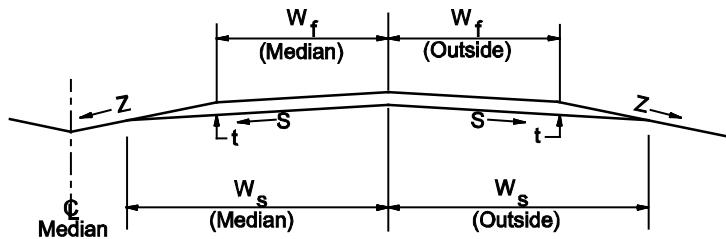
**Curve**

$$W_s(\text{median high side}) = W_f(\text{median}) + \frac{tZ}{1 + SZ}$$

$W_s(\text{outside low side})$  = same as tangent typical section width

$$W_s(\text{outside high side}) = W_f(\text{outside}) + \frac{tZ}{1 + SZ}$$

$W_s(\text{median low side})$  = same as tangent typical section width



Round all computed subgrade half widths to the nearest 0.1'.

**Intermediate (High Side).**

Compute the widths of intermediate surfacing courses for unsymmetrical sections on the high side in the same manner as for symmetrical sections (i.e., proportionately to the thicknesses), except that the width should be computed and recorded separately for each side of the centerline and rounded to the nearest 0.1'.

**Intermediate (Low Side).**

The following example (Example 13-3) illustrates the procedure that should be used to determine the widths for the intermediate surface courses on the low side of superelevated curves:

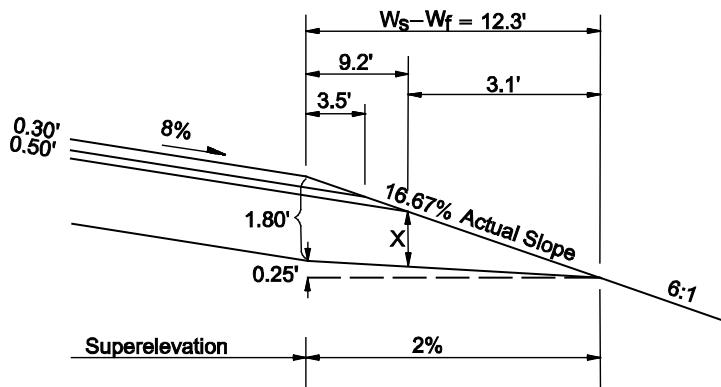
**Example 13-3: Unsymmetrical Sections – Intermediate Surface Widths****Given:**  $t = 1.80$  feet $t_{x1} = 0.30$  feet $t_{x2} = 0.50$  feet $W_s = 32.3$  feet $W_f = 20.0$  feet

Superelevation rate = 8%

Subgrade shoulder slope = 2%

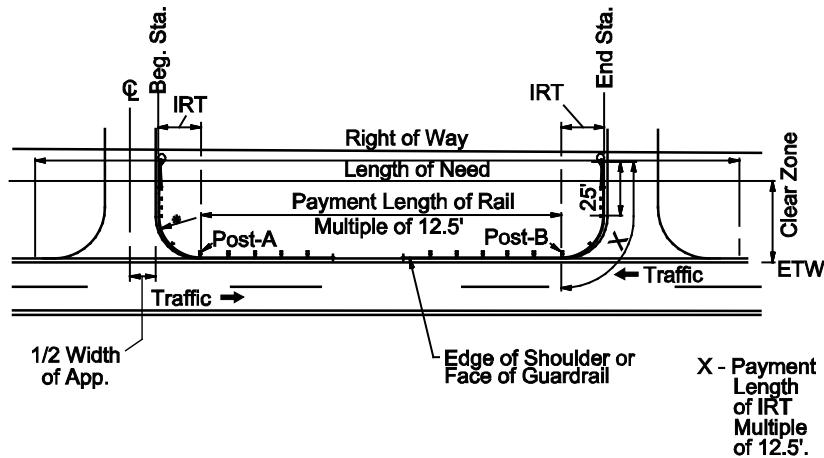
**Problem:** Determine the widths for the intermediate surface lifts.**Solution:**1. Determine the actual slope rate.Subgrade shoulder width =  $W_s - W_f = 12.3'$ Rise of subgrade =  $12.3' \times 0.02 = 0.246' \approx 0.25'$ Total depth =  $0.25' + 1.80' = 2.05'$ Actual slope =  $2.05' \div 12.3' = 0.1667$ , or 16.67%

(Rounded to the nearest 0.01%)

2. Determine horizontal distance for intermediate lifts.Slope difference =  $(16.67 - 8.00) \div 100 = 0.0867$  $t_{x1} \div$  slope difference =  $0.30' \div 0.0867 = 3.46' \approx 3.5'$  $(t_{x1} + t_{x2}) \div$  slope difference =  $(0.30' + 0.50') \div 0.0867 = 9.23' \approx 9.2'$ 

## GUARDRAIL QUANTITIES BACKGROUND

1. All w-beam, box beam, and cable guardrail runs are measured by the length of feet, exclusive of terminal sections or transitions including Intersecting Roadway Terminals (IRT). One-way departures, Optional Terminal Sections (OTS), and all transitions (including Bridge Approach Sections) are measured per each.
2. Lengths of w-beam guardrail should be rounded up to 12.5-foot increments. See the *MDT Detailed Drawings* for the length of each OTS.
3. Lengths of box beam guardrail should be rounded up to 18-foot increments, and the length of each box beam end section is 11.9 feet and requires at least one 18-foot section of standard box beam rail.
4. All one-way departure sections are located entirely outside the length of need. See the *MDT Detailed Drawings* for the length of need limits within Optional Terminal Section pay limits.
5. Rounding of guardrail to standard lengths will result in lengths of full strength rail that are greater than the measured length of need. When connecting to a fixed location, such as the end of a bridge rail, the stationing called out for guardrail will need to be established based on the bridge rail stationing. For other applications, providing the additional length to the advancement side of the adjacent traffic may be the best practice, however the location of approaches or other roadside features may dictate the optimum location. So long as the entire length of need is protected by full strength rail, and the rail length is at a standard increment, the end stations are not critical for these installations.
6. If approaches, turnouts or other obstacles are within the required length of w-beam guardrail, IRT terminals may be used to shorten the required length. IRTs do not meet all current crash testing requirements and should only be used as a best practical remaining alternative where fully compliant roadside hardware cannot address a guardrail warrant.

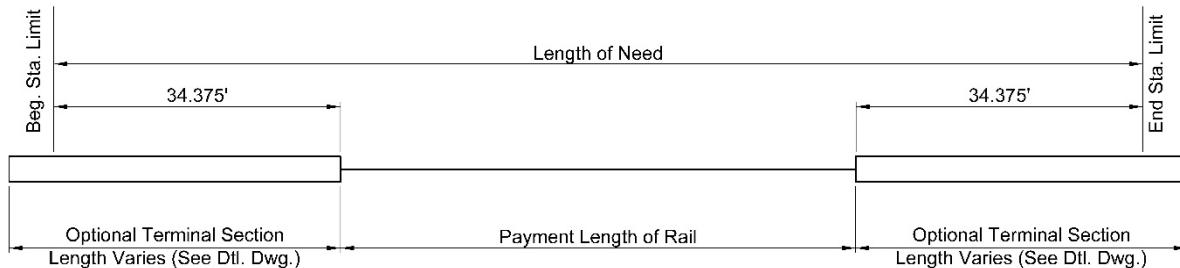


- a. Ensure that the right-of-way width is sufficient (i.e., far enough from the shoulder to get the full IRT installed without encroaching onto private property). The width required from the edge of the roadway (face of rail) to the R/W line is equal to the IRT radius + 26.5 feet.

- b. Determine the best fit IRT radius based on the approach radii, R/W availability, and the location requirements of the normal run of w-beam. Minor adjustments to the approach stationing or minor grading along the edge of the approach may be necessary to fit the IRT to the approach without impacting turning movements or extending beyond the R/W limit.
- c. The end anchors are included in the IRT bid item.
- d. See the *MDT Detailed Drawings* for available IRT radii and associated pay limits.

**Example 13-4: W-Beam Guardrail**

**Given:** W-beam guardrail is warranted between Stations 9+90 and 15+00 on the left side of a two-way roadway. There are no roadway approaches or other features that influence the guardrail location.



**Problem:** Determine the beginning and ending stations and the length of rail for payment.

**Solution:**

1.  $[15+00.00] - [9+90.00] = 510.00'$  actual length of need
2. Per the detailed drawings, 34.38' of each OTS provides full strength for length of need.
3.  $510.00' - 2(34.38) = 441.24'$  length of standard run MGS rail requirement
4.  $441.24' \div 12.5'/\text{section} = 35.3$  sections, Round  $\Rightarrow 36$
5.  $36 \times 12.5' + 2(34.38) = 518.76'$  Length of need based on minimum standard increment
6. In this case, no features have been identified to restrict guardrail placement. Locate the guardrail to provide the additional length on the advancement side of the adjacent traffic. Since the rail is on the left side of the roadway, adjacent traffic is moving opposite the direction of increasing stationing, therefore start the calculation from the lower station value:

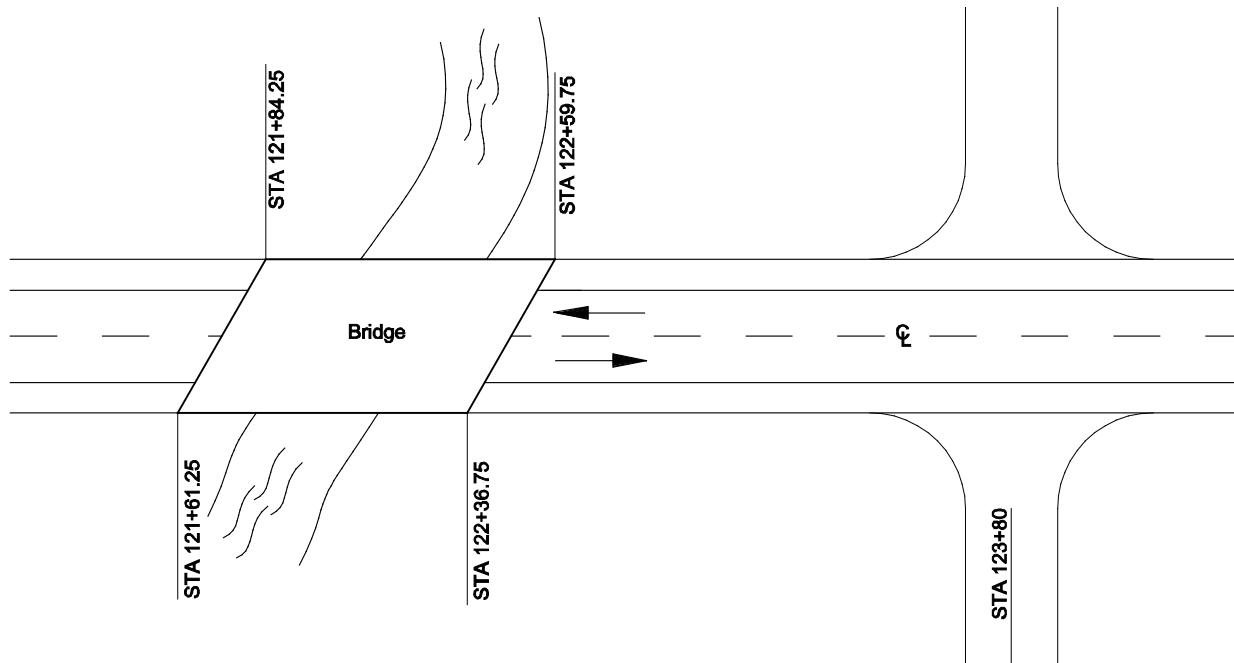
$9+90.00 =$  Beginning Station in plans (Please note, there is additional length of OTS beyond this station)

$[9+90.00] + (36 \times 12.5' \text{ w-beam}) + (2 \times 34.38' \text{ full strength portion of OTS})$   
 $= 15+08.76$  Ending Station in plans (Please note, there is additional length of OTS beyond this station)

**Additional discussion:** If the rail had been on the right side, providing the additional length on the advancement side of the adjacent traffic would be calculated from the end station of the length of need working back on stationing (15+00.00 back to 9+81.24).

### Example 13-5: Computations of Pay Quantities for W-Beam Guardrail and Intersecting Roadway Terminal (IRT) Sections

**Given:** A bridge replacement project (on a two-way, two-lane highway) calls for guardrail lengths of need from the end of the bridge rail of 141.5 feet and 76.2 feet, for the approach and departure sides respectively. (See Example 9-3). The roadway width is 40 feet (12 foot lanes and 8 foot shoulders) and R/W is 80 feet from centerline on each side of the road. There are private approaches needed on each side of the roadway at station 123+80. The approaches are currently designed 24 feet wide with 25 foot radii per *MDT Detailed Drawings* and cannot be relocated beyond minor adjustments.



**Problem:** Determine appropriate w-beam guardrail treatment for the end of the bridge with the private approaches, and determine the station limits and quantities for the guardrail.

#### Solution:

1. Determine the appropriate treatment for the bridge approach rail connecting to the bridge rail on the right side:

Calculate the available distance from the end of the bridge rail to the beginning of the approach radius.

Approach station [123+80.00] – 12' half approach width – 25' radius = begin of radius station [123+43.00]

Begin of radius station [123+43.00] – end of bridge rail station [122+36.75] = 106.25' of available space.

Divide the departure length of need by the standard increment to determine the full strength guardrail needed.

$$76.2' - 34.38' \text{ (OTS)} - 37.5' \text{ (Bridge Approach Section)} = 4.32'$$

$4.32' \div 12.5'/\text{section} = 0.35 \text{ sections}$ , Round  $\Rightarrow 1 \text{ section of standard MGS rail for length of need}$

Since up to 16.42' of a MGS OTS is not full strength, add 16.42' to the needed guardrail length.

$$(1 \text{ section} \times 12.5'/\text{section}) + 34.38' + 37.5' + 16.42' = 100.8'$$

100.8' of needed guardrail  $< 106.25'$  of space available, therefore use standard w-beam approach rail with a Bridge Approach Section and OTS.

The guardrail on the right side will be from station 122+36.75 to 123+37.55 and will include one 37.5-foot Bridge Approach Section (bid per each), one OTS (bid per each), and 12.5 feet of w-beam. However, for stationing in the plans, remove the additional 16.42' and station to length of need (123+21.13).

2. Determine the appropriate treatment for the bridge approach rail connecting to the bridge rail on the left side:

Calculate the available distance from the end of the bridge rail to the beginning of the approach radius.

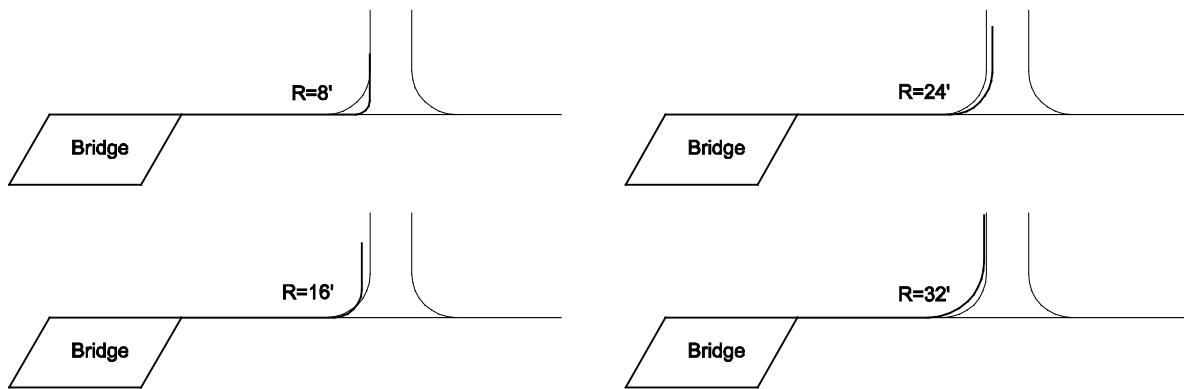
Begin of radius station [123+43.00] – end of bridge rail station [122+59.75] = 83.25' available. This distance is not long enough to allow the minimum length of blunt end protection with an OTS for the bridge end (37.5' Bridge Approach Section and up to 50.8' OTS). This option also does not provide the calculated advancement length needed for shielding the crossing hazard.

Determine a bridge approach rail solution using an IRT:

The edge of the current approach station is [123+80.00] – 12' half width of approach = [123+68.00]

The space for rail with an IRT = [123+68.00] - [122+59.75] = 108.25'

IRT radii are available in increments of 8 feet, up to 32 feet. Subtracting each radius from the space available leaves available lengths of tangent guardrail of 100.25', 92.25', 84.25', and 76.25'. The closest fit configuration for each IRT radius option is shown below (approach end is at the R/W limit for all cases).



For this example, all options fit within the available R/W and could potentially be used with minor widening, narrowing, and/or relocation of the approach location. In this instance, the 24 foot radius was selected (with the approach being relocated 4 feet ahead on station), based on the anticipated traffic needs. Selecting this option does not require any additional width in guardrail widening in front of the rail or a reduction in approach radius. It also provides nearly 10 feet of space between the R/W line and the end of rail for maintenance/utility access.

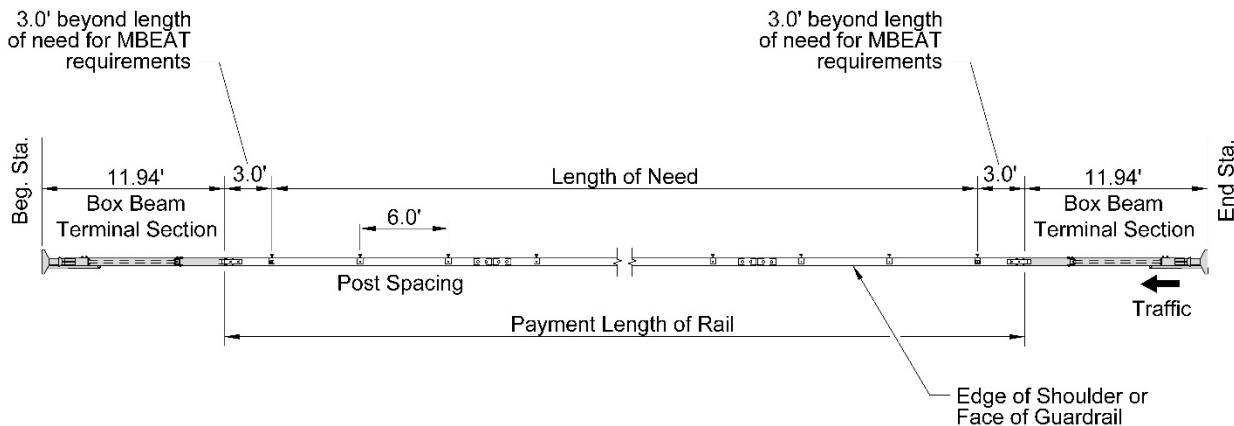
Determine stationing:

$$[122+59.75] + 37.5' \text{ (bridge approach section)} + 50' \text{ (standard MGS rail)} + 24' \text{ (IRT radius)} = \\ [123+71.25]$$

The guardrail on the left side will be from station 122+59.75 to 123+71.25 and will include one 37.5-foot Bridge Approach Section (bid per each), 50 feet of standard MGS rail, and 62.5 feet of Intersecting Roadway Terminal.

**Example 13-6: Box Beam Guardrail**

**Given:** Box Beam guardrail is warranted between Stations 17+50.00 and 32+75.00. The facility is a two-lane, two-way roadway requiring a terminal section (MBEAT) at each end, and there is a private approach at station 33+40 on the same side of the roadway as the guardrail.



**Problem:** Determine the beginning and ending stations and the length of rail for payment.

**Solution:**

1.  $[(32+75.00) - (17+50.00)] + (2)(3' \text{ beyond length of need for MBEAT requirements}) \div 18' \text{ increment} = 85.06 \text{ sections, Round} \Rightarrow 86 \text{ sections of Box Beam guardrail}$
2.  $86 \times 18' = 1,548.0' \text{ Payment Length of Box Beam Guardrail}$
3. Because of the approach located at station 33+40, locate the rail as far back on stationing as possible to reduce impacts to sight distance and turning maneuvers associated with the approach.  
 $[32+75.00] + 3' + 11.94' \text{ of terminal outside of length of need} = 32+89.94 \text{ Ending Station}$   
 $[32+89.94] - 1548.0' \text{ of standard run rail} - (2 \times 11.94' \text{ MBEAT length}) = 17+18.06 \text{ Beginning Station}$
4. 2 Box Beam MBEAT terminal sections bid per each

### Example 13-7: Topsoil Replacement Quantities

**Given:** A rural reconstruction project, utilizing unclassified excavation with 20% shrink and with the following topsoil and seeding quantities:

TOPSOIL & SEEDING										
STATION		cubic yards	acres							REMARKS
			SEED			CONDITION SEEDBED	MULCH			
FROM	TO	TOPSOIL SALVAGING & PLACING	NO. 1	NO. 2	NO. 3	NO. 1	NO. 2	EROSION CONTROL BLANKET (LONG-TERM)		
53+81.86	83+00.00	1,450	4.4	2.0	0.2	4.4	2.0	4.6	2.0	
83+00.00	113+00.00	2,348	0.2	6.2	2.1	0.2	6.2	2.3	6.2	
93+52.02	94+01.48									106 BRIDGE END GRADING EROSION CONTROL
113+00.00	143+00.00	721	0.3		1.0	0.3		1.3		
143+00.00	170+19.65	767	5.2		1.5	5.2		6.7		INCLUDES CONNECTION TO PTW
TOTAL		5,286	10.1	8.2	4.8	10.1	8.2	14.9	8.2	106

**Problem:** Determine the topsoil replacement quantities.

**Solution:** Topsoil replacement is a grading quantity that is needed to adjust the earthwork on a project to account for the topsoil that is salvaged from the roadway construction limits prior to the general grading operation. This material was in place when the project was surveyed and the digital terrain model (DTM) was created, and is included in the line representing the existing ground to which cut and fill quantities are measured. The removal of this material prior to grading has the effect of lowering the existing ground line wherever it is removed, thereby underestimating the amount of embankment needed in fill sections, and overestimating the amount of material generated from cut sections. For either condition, embankment material must be added to the earthwork run to account for the topsoil that is removed.

To estimate the amount of embankment required for topsoil replacement, the quantity of topsoil salvaged needs to be adjusted by the project shrink factor. The Standard Specifications require that the contractor salvage enough topsoil from within the construction limits to dress the finished slopes with four inches of topsoil. For this reason, the depth, quality and distribution of the topsoil on the existing slopes is somewhat irrelevant. Similarly, areas where topsoil is not removed (e.g. Foundation Treatment areas) do not typically need special consideration when calculating Topsoil Salvaging and Placing quantities. The Topsoil Salvaging and Placing quantities have already been calculated for this example and are indicated in the summary frame above. Although the Summary is Topsoil & Seeding, the quantity splits are intended to aid in calculating topsoil replacement grading quantities, and to show the distribution of these quantities more uniformly in the mass diagram and earthwork run.

Since grading on this project is measured as Unclassified Excavation, an earthwork run and mass diagram are developed. The unadjusted quantities of topsoil salvage should be entered into the earthwork run as point additional embankment quantities for each section, and adjusted according to the project shrink factor. It isn't critical whether the "from" or "to" station is used to identify the locations where these quantities are added in the earthwork run, only that the method used is consistent for the project.

ADDITIONAL GRADING					
STATION		cu. yards		REMARKS	
		INCL. IN ROADWAY			
		UNCL. EXC.	EMB. +	ADD. UNCL. EXC. #	
FROM	TO				
			6,345		TOPSOIL REPLACEMENT
60+91.00		15	230		FARM FIELD APP. RT.
61+78.00	64+63.90	*	*		MAILBOX TURNOUT LT.
63+08.00		25	5		PRIVATE APP. LT.
69+26.00	72+12.00	*	*		MAILBOX TURNOUT RT.
70+83.00		30	80		PRIVATE APP. RT.
78+77.00		15	70		PRIVATE APP. LT.
81+11.44	93+50.02 BE		155		GUARDRAIL WIDENING RT.
82+60.65	93+50.02 BE		135		GUARDRAIL WIDENING LT.
93+50.02 BE	94+03.48 BE	930	10	150	BRIDGE END GRADING - SEE DETAIL
93+87.00		15			GR. TO DR. DT. RT. - SEE DETAIL
94+03.48 BE	96+92.10		40		GUARDRAIL WIDENING LT.
94+03.48 BE	102+06.85		105		GUARDRAIL WIDENING RT.
99+27.00		50	5		PRIVATE APP. LT. - 48' WIDE
102+35.00		80	520		PRIVATE APP. RT.
107+00.00		170			PRIVATE APP. LT.
143+25.00		225	15		FARM FIELD APP. RT. - 12' WIDE
147+95.00		300			FARM FIELD APP. LT. - 12' WIDE
153+30.00		10	2,610		PRIVATE APP. LT. (MT DNRC)
163+66.00	166+50.00	*	*		MAILBOX TURNOUT LT.
<b>TOTAL</b>		<b>1,865</b>	<b>10,325</b>	<b>150</b>	

\* INCLUDED IN MAINLINE GRADING

# EXCAVATION QUANTITY - MATERIAL IS UNSUITABLE FOR ROADWAY EMBANKMENT

**Additional discussion:** For projects measuring grading as Embankment-in-Place, the entire quantity of topsoil salvaged is identified on a separate line of the Grading Frame, and identified as "TOPSOIL REPLACEMENT" in the Remarks column. For these projects, no adjustments to grading are made, and additional grading items are not included in the earthwork run.